

Recent results on exotic hadrons at LHCb

Giovanni Cavallero on behalf of the LHCb collaboration

University of Genova and INFN





CERN-LHC seminar, October 30, 2018

Outline

- overview on exotic hadrons
- the LHCb detector
- highlights of LHCb results on exotic spectroscopy
- evidence for an $\eta_c(1S)\pi^-$ resonance in $B^0 o \eta_c(1S) K^+\pi^-$ decays
- model-independent evidence for exotic contributions in $B^0 \to J/\psi K^+\pi^-$ decays

Introduction

 hadrons beyond conventional mesons and baryons foreseen since the formulation of the constituent quark model in 1964

AN SU3 MODEL FOR STRONG INTERACTION SYMMETRY AND ITS BREAKING II $^{*)}$

A SCHEMATIC MODEL OF BARYONS AND MESONS *

M. GELL-MANN California Institute of Technology, Pasadena, California

Received 4 January 1964

anti-triplet as anti-quarks \bar{q} . Baryons can now be constructed from quarks by using the combinations (qqq), (qqqq), etc., while mesons are made our of (q \bar{q}), (qq $\bar{q}\bar{q}$), etc. It is assuming that the lowes

G. Zweig CERN-Geneva

In general, we would expect that baryons are built not only from the product of three moses, AAA, but also from AAAAA, matAAAAA, etc., where $\overline{\Lambda}$ denotes an anti-acce. Similarity, meson could be formed from $\overline{\Lambda}$, AAAA etc. For the low mass mesons and baryons we will assume the simplest possibilities, $\overline{\Lambda}$ and AAA, that is, "denote mat three".

- not forbidden by QCD as long as they form colour-singlet configurations
- many searches for exotic hadrons in the light-spectroscopy sector without success:
 - experimentally difficult given the high density of broad and overlapping states, and the large backgrounds
 - theoretical predictions are challenging given the relativistic *u*, *d* and *s* constituents
- since 2003, about thirty hadrons not fitting with the conventional heavy-quarkonium states have been observed

Heavy-quarkonium spectra

[S. L. Olsen, T. Skwarnicki, and D. Zieminska, Rev. Mod. Phys. 90 (2018) 015003]



- large *c* and *b*-quark masses allow to treat charmonium (*cc̄*) and bottomonium (*bb̄*) mesons as **non-relativistic systems** ⇒ simpler systems ⇒ spectra of observed states well described by QCD motivated potential models with corrections provided by the NRQCD framework (dashed lines)
- narrow and non-overlapping states
- limited number of unassigned states below open-flavour thresholds
- no mixing with lighter quarkonium states

Heavy-quarkonium-like spectra

[S. L. Olsen, T. Skwarnicki, and D. Zieminska, Rev. Mod. Phys. 90 (2018) 015003]



- plethora of unexpected neutral (X,Y) and charged (Z^+, P_c^+) states discovered by *B*-, *c* and τ factories and by experiments at hadronic colliders
- their decay modes indicate they must contain an heavy quark-antiquark pair in their internal structure
- but either their mass, decay properties or electric charge are not consistent with unassigned charmonium or bottomonium levels

\Rightarrow more complex substructure than heavy-quarkonium states

Interpretations of exotic hadrons

• four-quark candidates classified as X (neutral), Y (neutral and $J^{PC} = 1^{--}$) and Z (charged); pentaquark candidates named P

- different models have been proposed about the quark composition and binding mechanisms of these exotic hadrons
- a clear pattern is missing: experimental and theoretical efforts are needed to understand their nature
- it is important to search for new exotic candidates along with new production mechanisms and decay modes of already observed unconventional states
- many contributions from the LHCb experiment



The LHCb experiment

The LHCb experiment

[JINST 3 (2008) S08005]

By design: study CP-violating processes and rare *b*- and *c*-hadrons decays



- VELO: excellent resolution on primary and secondary vertex separation
- **RICH 1 and 2**: optimal charged hadrons discrimination over the 10 range
- Muon stations: ~ 90% efficiency on muon triggers

Recent results on exotic hadrons at LHCb

The LHCb data taking and physics

- Run 1: $\sim 3 \, {
 m fb}^{-1}$ of pp collisions at $\sqrt{s} =$ 7-8 ${
 m TeV}$
- Run 2: ~ 6 fb⁻¹ of pp collisions at $\sqrt{s} = 13 \text{ TeV}$ ($\sigma_{b\bar{b}} \propto \sqrt{s} \Rightarrow 4x \ b\bar{b}$ pairs with respect to Run 1)



Thanks to the LHC!

Excellent tracking and PID performance \Rightarrow extended Physics programme

⇒ not only CP violation and rare decays measurements, but also LFU tests, exotic and conventional spectroscopy, production and polarisation measurements, EW and QCD physics, dark photon searches, p-Pb and p-He physics, ...

Exotic hadrons at LHCb: highlights

LHCb contributions to the understanding of the X(3872) state

- first exotic candidate observed by Belle in 2003 [Belle collaboration, Phys. Rev. Lett. 91 (2003) 262001]
- quantum numbers measurements $\Rightarrow J^{PC} = 1^{++}$ [Phys. Rev. D92 (2015) 011102], [Phys. Rev. Lett. 110 (2013) 222001]
- search for new decay modes [EPJC 73 (2013) 2462], [Phys. Lett. B 769 (2017) 305]
- direct production in pp collisions [EPJC 72 (2012) 1972]



• measurement of $\mathcal{B}(X(3872) \rightarrow \psi(2S)\gamma)/\mathcal{B}(X(3872) \rightarrow J/\psi\gamma))$: disfavors the pure $D\bar{D}^*$ molecular integretation [Nucl. Phys. B 886 (2014) 665]

 \Rightarrow strong indications that the X(3872) is a **quantum mixture** of the $\chi_{c1}(2P)$ charmonium state (accounting for the prompt production rate) with a $D^0 \bar{D}^{*0}$ molecule state (accounting for the isospin violation coming from the observation of the decays to $J/\psi\rho$ and $J/\psi\omega$)

[M. Padmanath, C. B. Lang, and S. Prelovsek, Phys. Rev. D92 (2015) 034501]

Recent results on exotic hadrons at LHCb

Giovanni Cavallero

October 30, 2018

Confirmation of the $Z_c(4430)^+$ state in $B^0 o \psi(2S) K^+ \pi^-$ decays

[Phys. Rev. Lett. 112 (2014) 222002]

- confirmation of the existence of the $Z_c(4430)^+$ charged charmonium-like state, and determination of its $J^P = 1^+$ quantum numbers with very high significance
- first unambiguous exotic state
- demonstration of its **resonant character** through the study of the Argand diagram
- model-independent approach used to demonstrate that the $\psi(2S)\pi^-$ structures can not be explained by reflections from $K^+\pi^-$ contributions alone [Phys. Rev. D92 (2015) 112009]



Discovery of two pentaquark candidates in $\Lambda_b \rightarrow J/\psi p K^+$ decays [Phys. Rev. Lett. 115 (2015) 072001]

- first observation of two pentaquark candidates $P_c(4450)^+$ and $P_c(4380)^+$ using Run 1 data ($\approx 26000 \Lambda_b \rightarrow J/\psi p K^+$ decays)
- Argand plot consistent with a resonance for the $P_c(4450)^+$, not conclusive for the $P_c(4380)^+$
- P⁺_c states have opposite parities
- supported by a model-independent analysis [Phys. Rev. Lett. 117 (2016) 082002]
- evidence for pentaquark contributions also in the Cabibbo-suppressed $\Lambda_b \rightarrow J/\psi p \pi^+$ decay mode [Phys. Rev. Lett. 117 (2016) 082003]



Recent results on exotic hadrons at LHCb

October 30, 2018

Neutral exotics in $B^+ \rightarrow J/\psi \phi K^+$ decays

[Phys. Rev. Lett. 118 (2016) 022003], [Phys. Rev. D95 (2016) 012002]

- confirmation of the X(4140) and X(4274) states
- discovery of two higher mass states: X(4400) and X(4700)
- quantum numbers assignments



• $D_s^+ D_s^{*-}$ cusp model included among systematic variations [E. S. Swanson, Int. J. Mod. Phys. E25 (2016) 1642010]



 indications that the X(4140) may not be a bound state that can be described by the Breit–Wigner function

Recent results on exotic hadrons at LHCb

Searches for exotic hadrons containing b quarks

Search for weakly decaying *b*-flavoured pentaquarks [Phys. Rev. D97 (2018) 032010]

Run 1 data $\Rightarrow L \sim 3 \, {\rm fb}^{-1}$



Upper limits relative to Λ_b production times its branching fraction to $J/\psi p K^+$ of $\mathcal{O}(10^{-3})$

Search for $X_{b\bar{b}b\bar{b}} \rightarrow \Upsilon(1S)\mu^+\mu^-$ [JHEP 10 (2018) 086]

2011–2017 data $\Rightarrow L \sim 6.3 \, {\rm fb}^{-1}$

No significant excess for any mass hypothesis between 17.5 and 20.0 GeV



Upper limits on production cross section of $\mathcal{O}(10\,\mathrm{fb})$

Evidence for an $\eta_c(1S)\pi^-$ resonance in $B^0 \rightarrow \eta_c(1S)K^+\pi^-$ decays

[arXiv:1809.07416]

Accepted by EPJC

Motivations

[arXiv:1809.07416]

- prediction of states decaying to $\eta_c(1S)\pi^-$ depending on the model used to described the $Z_c(3900)^-$, discovered by BESIII [BESIII collaboration, Phys. Rev. Lett. 110 (2013) 252001]:
 - $Z_c(3900)^-$ as an hadrocharmonium state \Rightarrow charged charmonium-like state of mass $\approx 3800 \text{ MeV}$ [M. B. Voloshin, Phys. Rev. D87 (2013) 091501]
 - $Z_c(3900)^-$ as analogues of quarkonium hybrids \Rightarrow states with quantum numbers allowing the decay to $\eta_c(1S)\pi^-$ [E. Braaten, Phys. Rev. Lett. 111 (2013) 162003]
- the diquark model predicts a $J^P = 0^+$ exotic candidate decaying to $\eta_c(1S)\pi^-$ below the open-charm threshold [L. Maiani, F. Piccinini, A. D. Polosa, and V. Riquer, Phys. Rev. D71 (2005) 014028]

 \Rightarrow search for an $\eta_c(1S)\pi^-$ resonance studying $B^0 \rightarrow \eta_c(1S)K^+\pi^-$ decays



Recent results on exotic hadrons at LHCb

Analysis strategy [arXiv:1809.07416]

- the $\eta_c(1S)$ is reconstructed into the $p\bar{p}$ decay mode
- charged hadrons discrimination provided by the RICH detectors are of crucial importance to select and correctly identify $B^0 \rightarrow p\bar{p}K^+\pi^-$ decays
- isolate $B^0 \to \eta_c(1S)K^+\pi^-$ events from combinatorial and nonresonant $B^0 \to p\bar{p}K^+\pi^-$ decays
- perform a Dalitz plot analysis to search for exotic hadrons and measure quasi-two-body branching fractions
- use 2011–2016 data $\Rightarrow L \sim 4.7 \, \text{fb}^{-1}$



• Dalitz plot analysis performed separately for Run 1 and 2 data to take into account possible differences in the two data taking periods

Recent results on exotic hadrons at LHCb

Giovanni Cavallero

October 30, 2018

Signal yields

[arXiv:1809.07416]



- fit to the $m(p\bar{p})$ used to determine the $B^0 \rightarrow \eta_c(1S)K^+\pi^-$ branching fraction with respect to the $B^0 \rightarrow J/\psi K^+\pi^-$ normalisation channel
- reconstruction and selection efficiencies largely cancel in the ratio

•
$$R = \frac{N_{\eta_c}}{N_{J/\psi}} \times \frac{\epsilon_{J/\psi}}{\epsilon_{\eta_c}} = 0.357 \pm 0.015 \pm 0.008$$

$$\Rightarrow \mathcal{B}(B^0 o \eta_c(1S)K^+\pi^-) = (5.73 \pm 0.24 \pm 0.13 \pm 0.66) imes 10^{-4}$$

Recent results on exotic hadrons at LHCb

Amplitude analysis strategy

[arXiv:1809.07416]

- the $B^0 \rightarrow \eta_c(1S)K^+\pi^-$ decay involves only pseudoscalar particles \Rightarrow Dalitz plot (DP) analysis using the Laura++ package [Comput. Phys. Commun. 231 (2018) 198]
- the sizeable natural width of the η_c(1S) meson (Γ_{η_c} ~ 32 MeV) complicates the formalism:
 - the kinematic quantities entering the DP formalism are computed using $m(p\bar{p})$ instead of the known value of the $\eta_c(1S)$ mass
 - the natural width of the $\eta_c(1S)$ is set to zero when computing the DP normalisation (the effect of this simplification is taken into account when assessing systematic uncertainties)
- the isobar model is used to write the decay amplitude: $K^+\pi^-$ S-wave at $m(K^+\pi^-) \lesssim 1.7 \,\mathrm{GeV}$ parametrised with the LASS function, other resonances with relativistic Breit–Wigner functions
- simultaneous fit to Run 1 and Run 2 data using the JFIT framework [arXiv:1409.5080]: the signal and background yields, and the efficiency maps, are different between the two subsamples

Signal and background yields [arXiv:1809.07416]



- 2D fit to the joint $m(p\bar{p}K^+\pi^-) \times m(p\bar{p})$ distribution
- separate fit to Run 1 and 2 data samples
- D^0 and Λ_c^+ vetoes
- nonresonant and combinatorial backgrounds to be subtracted

Component	$\operatorname{Run} 1$	$\operatorname{Run}2$
$B^0 \rightarrow \eta_c K^+ \pi^-$	805 ± 48	1065 ± 56
$B^0 \rightarrow p \overline{p} K^+ \pi^-$ (NR)	234 ± 48	273 ± 56
Combinatorial background	409 ± 36	498 ± 41

Parametrisation of the backgrounds

[arXiv:1809.07416]

- use the sPlot technique to build the histograms for the nonresonant and combinatorial backgrounds
- parametrised using the Square Dalitz plot coordinates to avoid artefacts related to the curved boundaries of the DP
- smooth histograms through a cubic spline interpolation



Run 2

Background subtracted Dalitz plot

[arXiv:1809.07416]



Run 1 and 2

Efficiency parametrisation

[arXiv:1809.07416]

- the efficiency variation is caused by the detector acceptance and selection procedure
- use simulated samples generated uniformly across the Square Dalitz plot and correct for differences between data and simulation in the PID efficiencies using calibration samples
- smooth histograms through a cubic spline interpolation



Model with only $K^+\pi^-$ contributions [arXiv:1809.07416]



Recent results on exotic hadrons at LHCb

Giovanni Cavallero

October 30, 2018

Model with $K^+\pi^-$ and $\eta_c(1S)\pi^-$ contributions [arXiv:1809.07416]



Recent results on exotic hadrons at LHCb

Giovanni Cavallero

October 30, 2018

Systematic uncertainties

[arXiv:1809.07416]

experimental uncertainties:	Source	
 signal and background violds 	Nominal fit	
 backgrounds parametrisation efficiency parametrisation amplitude fit bias 	Fixed yields Phase-space border veto η_c width $K^+\pi^-$ S-wave	
model uncertainties:	Background	
• treatment of the $p_c(1S)$ natural	Source	
width	Default	
• $K^+\pi^-$ S-wave parametrisation	Fixed yields	
 fixed parameters of the 	Phase-space border veto	
resonances	η_c width	
 addition or removal of marginal 	Background	
	$K^+\pi^-$ S-wave	

• the systematic variations producing the largest deviations on the $Z_c(4100)^-$ parameters (mass, width and fit fraction) are used to evaluate the systematic effects on the significances

- $Z_c(4100)^-$ significance (top table) when including systematic uncertainties and correlations between them: 3.2σ
- Discrimination between $J^P = 0^+$ and $J^P = 1^-$ (bottom table) is not significant

components

 $\Delta(-2\ln\mathcal{L})$

41.4

45.8

44.6 36.6

31.8

27.4

 $\Delta(-2\ln\mathcal{L})$

18.6

23.8

24.4

4.2

3.4

1.4

Significance

 $\frac{4.8\sigma}{5.2\sigma}$

 5.1σ

 4.3σ

 3.9σ

 3.4σ

Significance

 4.3σ

 4.9σ

 4.9σ

 2.0σ

 1.8σ

 1.2σ

- addition of further high-mass ${\cal K}^{*0}$ states does not improve the quality of the fit
- additional amplitude decaying to $\eta_c(1S)\pi^-$ is not significant, nor an amplitude decaying to $\eta_c(1S)K^+$
- possible effect of the $\eta_c(1S)$ resonant phase motion in the overall amplitude is found negligible

$Z_c(4100)^-$ parameters and quasi-two-body branching fractions [arXiv:1809.07416]

•
$$m_{Z_c^-} = 4096 \pm 20^{+18}_{-22}$$
 MeV, $\Gamma_{Z_c^-} = 152 \pm 58^{+60}_{-35}$ MeV

quasi-two-body branching fractions measured by multiplying

$${\cal B}(B^0 o \eta_c(1S) K^+ \pi^-) = (5.73 \pm 0.24 \pm 0.13 \pm 0.66) imes 10^{-4}$$

with the fit fractions resulting from the Dalitz plot fit

Decay mode	Branching fraction (10^{-5})	
$B^0 \to \eta_c K^*(892)^0 (\to K^+ \pi^-)$	$29.5 \pm 1.6 \pm 0.6 {+1.0 \atop -2.8} \pm 3.4$	
$B^0 \to \eta_c K^* (1410)^0 (\to K^+ \pi^-)$	$1.20 \pm 0.63 \pm 0.02 \pm 0.63 \pm 0.14$	
$B^0 \to \eta_c K^+ \pi^- (\text{NR})$	$5.90 \pm 0.84 \pm 0.11 \ ^{+0.57}_{-0.69} \ \pm 0.68$	
$B^0 \to \eta_c K_0^* (1430)^0 (\to K^+ \pi^-)$	$14.50 \pm 2.10 \pm 0.28 \ ^{+2.01}_{-1.60} \ \pm 1.67$	
$B^0 \to \eta_c K_2^* (1430)^0 (\to K^+ \pi^-)$	$2.35 \pm 0.87 \pm 0.05 \ ^{+0.57}_{-0.92} \ \pm 0.27$	
$B^0 \to \eta_c K^* (1680)^0 (\to K^+ \pi^-)$	$1.26 \pm 1.15 \pm 0.02 \ ^{+0.86}_{-0.97} \ \pm 0.15$	
$B^0 \to \eta_c K_0^* (1950)^0 (\to K^+ \pi^-)$	$2.18 \pm 1.04 \pm 0.04 \ ^{+0.80}_{-1.43} \ \pm 0.25$	
$B^0 \to Z_c(4100)^- K^+$	$1.89 \pm 0.64 \pm 0.04 \ ^{+0.69}_{-0.63} \ \pm 0.22$	

statistical, branching fraction systematic, fit fraction systematic, external branching fractions uncertainties

Model-independent evidence for exotic contributions in $B^0 \rightarrow J/\psi K^+\pi^-$ decays

Motivations

- $Z_c(4430)^-$ discovered in the $Z_c(4430)^-
 ightarrow \psi(2S)\pi^-$ decay mode
- $Z(4430)^- \rightarrow J/\psi \pi^-$ decay mode not yet confirmed: the understanding of this would provide insights into the internal structure of the $Z(4430)^-$
- in the dynamical diquark picture, this suppression is explained by a better overlap of the $Z(4430)^-$ radial wavefunction with the $\psi(2S)$ with respect to the radial ground J/ψ state [S. J. Brodsky, D. S. Hwang, and R. F. Lebed, Phys. Rev. Lett. 113 (2014) 112001]
- the Belle collaboration observed the $Z_c(4200)^- \rightarrow J/\psi\pi^-$ at 6.2 σ [Belle collaboration, Phys. Rev. D90 (2014) 112009]

Analysis strategy

- the $B^0\to J/\psi K^+\pi^-$ decay mode is dominated by $K^{*0}\to K^+\pi^-$ intermediate contributions
- given the low $Z(4430)^-$ fit fraction expected in this decay mode, an optimal description of the K^{*0} contributions would be required
- adopt the model-independent approach, only requiring the knowledge of the highest spin of the K^{*0} contributions for a given $m(K^+\pi^-)$ interval, to bypass the problem
- 4D angular analysis of $B^0 \rightarrow J/\psi K^+\pi^-$ decays to analyse the differential decay rate as a function of $m(K^+\pi^-)$ and of the three angles defining the decay
- test the hypothesis that the K^{*0} contributions alone can describe all the structures seen in the data using a novel 3D moments technique

Angular moments technique



- $\Omega = \{\theta_l, \theta_V, \chi\}$ characterise the decay for a $m(K^+\pi^-)$ value
- θ_V is the K^{*0} helicity angle tagging the spin J of the resonance

$$\left[\frac{\mathrm{d}\Gamma^k}{\mathrm{d}\Omega}\right]_{J_{\max}^k} \propto \sum_{i=1}^{n_{\max}^k} f_i(\Omega)\Gamma_i^k$$

- *f_i*(Ω) is an element of a set of orthonormal functions built starting from spherical harmonics of the three decay angles
- Γ_i^k are angular moments in the k^{th} bin of $m(K^+\pi^-)$ extracted from data (the dependence on $m(K^+\pi^-)$ can be neglected if the intervals are narrow)

Signal yields and K^{*0} **states** LHCb-PAPER-2018-043, in preparation

- large statistics of ~ 500k events with Run 1 data
- allows for independent fits in fine $m(K^+\pi^-)$ intervals (purity is larger than 90% for all of them)

•
$$J_{\max} = 2$$
 for $m(K^+\pi^-) < 1265 \, {
m MeV}$

•
$$J_{\max} = 3$$
 for $m(K^+\pi^-) > 1265 \,{
m MeV}$

- if only K^{*0} states contribute to the decay \Rightarrow data described by an expansion in angular moments with the sum truncated to J_{max}
 - if the data can be described only truncating the sum to unphysical high values for J_{max}, it is an indication of other dynamical processes contributing to the decay

Candidates / (8 MeV)



Recent results on exotic hadrons at LHCb

Model from angular moments

- use simulated events generated flat in the angular space and including efficiency effects
- weight events using normalised moments determined from data



Significance and results

LHCb-PAPER-2018-043, in preparation



⇒ the profile likelihood ratio test demonstrates at more than 5σ that K^{*0} contributions alone cannot describe the dynamics of the $B^0 \rightarrow J/\psi K^+\pi^-$ decay



By inspecting the DP, structures are visible at $m(J/\psi\pi^-) \approx 4200 \text{ MeV}$ and $m(J/\psi\pi^-) \approx 4600 \text{ MeV}$

The nature of the non- K^{*0} contributions can be investigated with a future amplitude analysis

Conclusions

- the study of exotic spectroscopy is important to improve the understanding of the non-perturbative regime of QCD
- the LHCb collaboration already provided important results in this sector, and will contribute further in the near future with important updates using the Run 2 data sample
- LHCb is going to be upgraded, *i.e.* a brand new detector will be built, implementing an innovative software-based trigger system, that will improve the efficiency on hadronic final states and will make it possible to collect a larger data sample exploiting the increased instantaneous luminosity

Thanks!

Backup slides

$Z_c(4100)^-$ significance determination strategy

- generate 1000 toys according to the no-Z model
- fit with both the no-Z (H₀) and Z (H₁) models and determine $\lambda = -2 \ln \frac{\mathcal{L}(H_0)}{\mathcal{L}(H_1)} = \Delta(-2 \log \mathcal{L})$
- when fitting with H_0 , add the $Z_c(4100)^-$ component but fixing its isobar coefficients to zero (assure the regularity of the likelihood around the point of constraint)
- when fitting with H_1 , $Z_c(4100)^-$ mass and width are left floating \Rightarrow look-elsewhere effect taken into account
- check $\Delta(-2\log \mathcal{L})$ follows a χ^2 distribution
- fit Δ(-2 log L) to determine the number of degrees of freedom: a χ² with ndof=8 describes well Δ(-2 log L)

$$n_{\sigma}(\Delta(-2 \ln \mathcal{L}) = \sqrt{2} \text{ TMath::ErfcInverse}(\text{TMath::Prob}(\Delta(-2 \ln \mathcal{L}), 8))$$
 (1)

Recent results on exotic hadrons at LHCb

Giovanni Cavallero

October 30, 2018

$\Delta(-2 \ln \mathcal{L})$ for $J^P = 0^+$



Recent results on exotic hadrons at LHCb

40/37

$\Delta(-2 \ln \mathcal{L})$ for $J^P = 1^-$



Recent results on exotic hadrons at LHCb

$Z_c(4100)^-$ quantum numbers: significance determination strategy

- generate 1000 toys according to $J^P = 0^+$ hypothesis
- fit with both the $J^P = 0^+$ (H_0) and $J^P = 1^-$ (H_1) models and determine $\lambda = -2 \ln \frac{\mathcal{L}(H_0)}{\mathcal{L}(H_0)} = \Delta(-2 \log \mathcal{L})$
- lower limit on the significance of the rejection of the $J^P = 0^+$ hypothesis:

$$n_{\sigma} = \sqrt{\Delta(-2\ln\mathcal{L})} \tag{2}$$



Signal and background yields: 2D fit for Run 2 [arXiv:1809.07416]



Square Dalitz plot coordinates and helicity angle

$$m' \equiv \frac{1}{\pi} \arccos\left(2\frac{m(K^{+}\pi^{-}) - m_{K^{+}\pi^{-}}^{\min}}{m_{K^{+}\pi^{-}}^{\max} - m_{K^{+}\pi^{-}}^{\min}} - 1\right)$$
$$\theta' \equiv \frac{1}{\pi}\theta(K^{+}\pi^{-}),$$



Recent results on exotic hadrons at LHCb

Giovanni Cavallero

October 30, 2018

 $K^+\pi^-$ model: log $m(K^+\pi^-)$ [arXiv:1809.07416]



 $K^+\pi^-$ model: log $m(\eta_c(1S)\pi^-)$ [arXiv:1809.07416]



 $K^+\pi^-$ model: log $m(\eta_c(1S)K^+)$ [arXiv:1809.07416]



 $K^+\pi^-$ model: 2D pull [arXiv:1809.07416]



Recent results on exotic hadrons at LHCb

Giovanni Cavallero

October 30, 2018

 $\mathcal{K}^+\pi^-$ and $\eta_c(1S)\pi^-$ model: log $m(\mathcal{K}^+\pi^-)$ [arXiv:1809.07416]



 $\mathcal{K}^+\pi^-$ and $\eta_c(1S)\pi^-$ model: log $m(\eta_c(1S)\pi^-)$ [arXiv:1809.07416]



 $K^+\pi^-$ and $\eta_c(1S)\pi^-$ model: log $m(\eta_c(1S)K^+)$ [arXiv:1809.07416]



 $\mathcal{K}^+\pi^-$ and $\eta_c(1S)\pi^-$ model: 2D pull [arXiv:1809.07416]



$K^+\pi^-$ Legendre moments [arXiv:1809.07416]



$\eta_c(1S)\pi^-$ Legendre moments [arXiv:1809.07416]



$\eta_c(1S)K^+$ Legendre moments [arXiv:1809.07416]

