Indirect searches for Physics beyond the Standard Model with the LHCb experiment

## Johannes Albrecht (CERN)

B-Physik Seminar München, 07. Oktober 2011





#### ATLAS / CMS

A *unique* effort toward the high-energy frontier



Coutesy of G. Isidori, LP07









- The LHCb experiment
  - Overview of the experiment and performance
- Focus here on most promising searches:
  - Probe of Lorentz structure in  $B_d \rightarrow K^* \mu^+ \mu^-$  decays
  - Measurement of CP violation in B<sub>s</sub> mixing:  $B_s \rightarrow J/\psi \phi$ ,  $J/\psi f_0$
  - Probe an extended scalar sector:  $B_{s,d} \rightarrow \mu^+ \mu^-$
- Many interesting LHCb measurements not covered here
  - search for CPV in charm
  - Bs mixing in  $B_s \rightarrow \phi \phi$
  - radiative decays  $B_s \rightarrow K^* \gamma, \phi \gamma$
  - Progress towards the CKM phase  $\gamma$
  - Search for new penguin decays, for majorana neutrinos
  - production measurements, excited B's



## The LHCb Experiment: Overview of the experiment and performance



### The LHCb detector



- Huge cross sections:  $\sigma(pp \rightarrow bbX) @ 7 \text{ TeV} \sim 300 \ \mu b^*$ 
  - But only 1/200 events contain b quark → Trigger
- Large acceptance 1.9<η<4.9</li>
- Large boost:
  - average flight distance of B mesons ~ 10mm

→ A huge amount of very displaced b's

(\*) LHCb, Phys.Lett.B 694 (2010) 209

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### Keys for b-physics I: Trigger



L0 hardware	"high p <sub>T</sub> " signals in calorimeter and muon systems
HLT1 software	Partial reconstruction selection based on one or two tracks (dimuon) displaced in the VELO, muon ID (offline like)
HLT2 software	Global reconstruction (very close to offline) dominantly inclusive signatures

#### + Global event cuts rejecting busy events

	Charm	Hadr. B	Lept. B
Global efficiency	~10%	~40%	75-90%





Keys for b-physics II: mass resolution LM:  $\mu(B_d)$  and  $\mu(B_s)$ 







## Keys for b-physics III: IP and vertex resolution

### Primary vertex resolutions (25 tracks):

	LHCb [µm]	ATLAS [µm]	CMS [µm]
σ(x)	15.8	60	20-40
σ(y)	15.2	60	20-40
σ(z)	76	100	40-60



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### Keys for b-physics IV: Muon ID





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- - Momental Glooperation 0 19:49:24
  - 46 Event 143858637 IP: VELO (planes of silicon) which moves in to 8 mm from the LHC beams

2000 ب<sup>ي</sup>

0.0

Mar

May

(generated 2011-10-05 01:15 including fill 2181)

Jun

Jul

Month in 2011

Aug

Sep Oct

Apr

- Most of 2011, LHCb ran at 3.5x10<sup>32</sup>cm<sup>-2</sup>s<sup>-1</sup>
  - LHCb design luminosityprode100326mon 551 2<p<100 GeV/c



![](_page_9_Figure_7.jpeg)

![](_page_9_Picture_9.jpeg)

ATLAS

ALICE

CMS

LHCb

13h

10h

16h

19h

![](_page_10_Figure_0.jpeg)

ojections of the fit results in M<sub>B</sub> opo Johannes Albrecht

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![](_page_11_Figure_0.jpeg)

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### b fragmentation $f_d/f_s$

- Fraction of  $b \rightarrow B_s$  is an essential ingredient to  $B_s \rightarrow \mu\mu$  and other searches
- LHCb has measuredeatuin the data
  - Ratio of  $B \rightarrow D_s \mu X$  to  $B \rightarrow D^+ \mu X$  modes [LHCb-CONF-2011-028]
  - Ratio of  $B_d \rightarrow DK$  and  $B_s \rightarrow D_s \pi$  modes [Accepted by PRL]

 $B^{\upsilon} {\rightarrow} DK$  and  $B_{s} {\rightarrow} D_{s} \pi$   $_{[arxiv:1106.4435]}$ 

• Combination [LHCb-CONF-2011-034] Consistent results, combine B<sub>s</sub>/B<sup>0</sup> ratio f<sub>s</sub>/f<sub>d</sub>:

 $\left(\frac{f_s}{f_d}\right)_{\text{LHCb}}^{\text{TLHCb-CONF-2011-341}} = 0.267 \stackrel{+0.021}{-0.020}$ 

: similar to

LEP & Tevatron result:

- Found to be independent of  $PT.271 \pm 0.027$ 
  - Also similar to the test property and align to the property of the end of the property of the end of the property of the proper

![](_page_11_Figure_13.jpeg)

## New Lorentz structure: Angular analysis of $B^0 \rightarrow K^* \mu^+\mu^-$

![](_page_12_Figure_1.jpeg)

# CERNY

### New Lorentz structure: $B^0 \rightarrow K^* \mu^+ \mu^-$

![](_page_13_Figure_2.jpeg)

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# CERNY

### New Lorentz structure: $B^0 \rightarrow K^* \mu^+\mu^-$

![](_page_14_Figure_2.jpeg)

![](_page_15_Picture_0.jpeg)

### $B^0 \rightarrow K^* \ \mu^+ \mu^-$ in LHCb

- Select events with Boosted Decision Tree
  - Veto J/ $\psi$  and  $\psi$ (2S)
- Weight events according to ε<sup>-1</sup>
  - As function of  $(\theta_1, \theta_k, q^2)$
  - Procedure verified on  $B_d \rightarrow J/\psi K^*$  data and MC

![](_page_15_Figure_7.jpeg)

#### LHCb-CONF-2011-038

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![](_page_16_Picture_0.jpeg)

## $B^0 \rightarrow K^* \ \mu^+ \mu^-$ in LHCb

- Select events with Boosted Decision T
  - Veto J/ $\psi$  and  $\psi$ (2S)
- Weight events according to  $\varepsilon^{-1}$ 
  - As function of  $(\theta_l, \theta_k, q^2)$
  - Procedure verified on  $B_d \rightarrow J/\psi K^*$  data a
- Perform measurement in 6 q<sup>2</sup> bins using simultaneous fit of mass,  $\theta_l$  and  $\theta_k$ 
  - Differential BR dΓ/dq<sup>2</sup>
  - Longitudinal polarization F<sub>L</sub>
  - Forward backward assymmetry A<sub>FB</sub>
- [ Likelihood scan for F<sub>L</sub> and A<sub>FB</sub> due to correlations ]

![](_page_16_Figure_12.jpeg)

LHCb-CONF-2011-038

![](_page_17_Picture_0.jpeg)

## $\mathbb{B}^{0} \to \mathbb{K}^{*} \mu^{+} \mu^{-}$ in LHCb

![](_page_17_Figure_2.jpeg)

- Measurement based on 300 candidates (largest sample)
  - Purity comparable to B-factories
     Data in excellent agreement with SM predictions at current level of precision.
  - Generally statistics limited, systematic uncertainties small
     Next: add other observables such as AT<sup>(2)</sup>, sensitive to RH currents
- Data in excellent agreement with theory (☺ or ⊗ ?)

![](_page_18_Picture_0.jpeg)

## $B^0 \rightarrow K^* \ \mu^+ \mu^-$ in LHCb: next steps

![](_page_18_Figure_2.jpeg)

- Precisely determine the zero crossing point of A<sub>FB</sub>
- Measure A<sub>t</sub><sup>(2)</sup>, partial angular analysis
  - − 2/fb  $\rightarrow$  full angular analysis
- Many anaogue channels in preparation
  - $-~B_s\!\to \phi\mu^+\mu^-$  ,  $B^0\!\to K^*~e^+e^-$  ,  $\Lambda_B\to\Lambda~\mu^+\mu^-$
  - Isospin analyses

![](_page_18_Picture_11.jpeg)

# Search for NP in the Bs mixing phase: $B_s \rightarrow J/\psi\phi$ and $B_s \rightarrow J/\psi f_0$

![](_page_20_Picture_0.jpeg)

## CP violation in B<sub>s</sub> mixing

![](_page_20_Figure_2.jpeg)

- Interference between mixing and decay leads to CPV phase  $\phi_s = \phi_M 2\phi_D$
- Precise SM calculation for f<sub>s</sub> possible (small penguin contribution)

 $\phi_s^{SM}$  = -0.0363±0.0016rad

CKMFitter, hep-ph:0406184

- Additional contributions from New Physics possible φ<sub>s</sub>=φ<sub>s</sub><sup>SM</sup> +φ<sub>s</sub><sup>NP</sup>
- Requires time dependent, flavour tagged angular analysis

![](_page_20_Picture_9.jpeg)

## Experimental situation (before summer 2011)

Results presented before summer 2011 showed compatibility with SM at  $\sim 1\sigma$  but all experiments with the same trend....

![](_page_21_Figure_2.jpeg)

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![](_page_21_Picture_5.jpeg)

![](_page_22_Figure_0.jpeg)

gnal component

![](_page_23_Picture_0.jpeg)

LHCb has measured the Bs mixing frequency in  $B_s \rightarrow D_s^- \pi^+$  decays

![](_page_23_Figure_3.jpeg)

new WA: 
$$\Delta m_s^{
m WA} = 17.731 \pm 0.045~{
m ps}^{-1}$$

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lattice

exp

![](_page_24_Picture_0.jpeg)

### Time dependent CPV in Bs

![](_page_24_Figure_2.jpeg)

![](_page_25_Picture_0.jpeg)

### Time dependent CPV in Bs

$$\overline{B}_{s}^{0}\left\{\begin{array}{c} b \\ \overline{s} \\ W \\ W \\ \overline{s} \\ W \\ \overline{s} \\$$

- Narrow resonance  $\rightarrow$  clean
- Vector-vector final state
  - Requires time dependent angular analysis to separate CP even and CP odd
  - Measure also  $\Delta\Gamma$  directly

![](_page_25_Figure_7.jpeg)

![](_page_25_Figure_8.jpeg)

- Lower branching fraction (~1/4)
  - Higher background level
- Vector-pseudoscalar final state
  - No angular analysis needed
  - Needs  $\Delta\Gamma$  as input

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![](_page_25_Picture_16.jpeg)

![](_page_26_Figure_0.jpeg)

- Maximum likelihood fit with 10 physics parameters
  - 7 angular amplitudes and phases
  - $\Gamma_{s}, \Delta\Gamma_{s}, \phi_{s}$
- Proper time calibrated with prompt J/ $\psi$ :  $\sigma$ (t)~50ps
- Used Opposite sign flavour tagging, εD<sup>2</sup>=(2.08±0.41)%

![](_page_26_Figure_7.jpeg)

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![](_page_26_Picture_11.jpeg)

![](_page_27_Picture_0.jpeg)

## $B_s \rightarrow J/\psi \phi : \Delta \Gamma \text{ and } \phi_s$

![](_page_27_Figure_2.jpeg)

![](_page_28_Figure_0.jpeg)

## $B_s \rightarrow J/\psi f_0: \phi_s$

- LHCb made first observation of the decay  $B_s \rightarrow J/\psi f_0$
- Nice channel to measure  $\phi_s$  (CP odd eigenstate)
  - No need for angular analysis
  - But need to export  $\Gamma_s$ ,  $\Delta\Gamma_s$  & correlation matrix from  $B_s \rightarrow J/\psi \phi$

 $\phi_s = -0.44 \pm 0.44(stat) \pm 0.02(syst)$ 

LHCb-CONF-2011-051

![](_page_28_Figure_8.jpeg)

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2010 data

arXiv:1102:0206

## Combination of $\phi_s$ results

![](_page_29_Figure_1.jpeg)

Combine both results, simultaneous fit using joint likelihood

$$\phi_s = 0.03 \pm 0.16(stat) \pm 0.07(syst)$$

LHCb-CONF-2011-051

 $\phi_{s}^{SM} = -0.0363 \pm 0.0016$ rad

- Outlook:
  - 1/2 statistical uncertainty with 2011 data
  - Resolve ambiguity in  $\Delta\Gamma_{s}, \varphi_{s}$
  - Evaluate penguin contributions
  - Measurable with ~1/fb:  $A_{sl}$  and  $B_s \rightarrow \phi \phi$

![](_page_29_Picture_13.jpeg)

![](_page_30_Picture_0.jpeg)

## Artists impression: $\phi_s$ from LHC & Tevatron

![](_page_30_Figure_2.jpeg)

This is NOT an official accurate overlay – the experiments have not done this yet ! This is just flipping and scaling the PDFs taken from talks to give impression

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![](_page_31_Picture_0.jpeg)

# Search for the rare decays $B_s^0 \to \mu^+ \mu^-$ and $B^0 \to \mu^+ \mu^-$

arXiv:1103.2465 Phys. Lett. B 699 (2011) 330-340

LHCb-CONF-2011-047 will be submitted to PLB

370pb<sup>-1</sup>

37pb<sup>-1</sup>

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![](_page_32_Picture_0.jpeg)

Double suppressed decay: FCNC process and helicity suppressed:

→ very small in the Standard Model but well predicted:

Mode	SM
$B_s \rightarrow \mu^+ \mu^-$	3.2 ± 0.2 10 <sup>-9</sup>
${ m B}^0\!\!\rightarrow\mu^+\mu^-$	0.10 ± 0.01 10 <sup>-9</sup>

A.J.Buras: arXiv:1012.1447 E. Gamiz et al: Phys.Rev.D 80 (2009) 014503

![](_page_32_Figure_6.jpeg)

BR expressed in Wilson coefficients:

$$BR(B_q \to l^+ l^-) \approx \frac{G_F^2 \alpha^2 M_{B_q}^3 f_{B_q}^2 \tau_{B_q}}{64\pi^3 \sin^4 \theta_W} |V_{tb} V_{tq}^*|^2 \sqrt{1 - \frac{4m_l^2}{M_{B_q}^2}} \\ \left\{ M_{B_q}^2 \left( 1 - \frac{4m_l^2}{M_{B_q}^2} \right) c_S^2 + \left[ M_{B_q} c_P + \frac{2m_l}{M_{B_q}} (c_A - c_A') \right]^2 \right\}.$$

→ sensitive to contributions in the scalar/pseudo-scalar sector

 $\rightarrow$  highly interesting to probe **extended Higgs** models

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![](_page_32_Picture_13.jpeg)

![](_page_33_Figure_0.jpeg)

## $B_{s,d} \rightarrow \mu^+ \mu^-$ as probe for New Physics

Example: MSSM (with R-parity conservation)

$$BR(B_S \rightarrow \mu^+ \mu^-) \propto \frac{\tan^6 \beta}{m_A^4}$$

![](_page_33_Figure_4.jpeg)

→ limit or measurement of  $B_{s,d} \rightarrow \mu \mu$ will strongly constrain tan $\beta$  vs M<sub>A</sub> plane

### NUHM1

 $\tan\beta$  vs M<sub>A</sub> plane 60 tanβ ប៉ 0.9 Best fit contours in tan $\beta$  vs M<sub>A</sub> 50 0.8 plane in the NUHM1 model 0.7 40 [O. Buchmuller et al, arxiv:0907.5568] 0.6 30 0.5 0.4 20 0.3 0.2 CMS direct search 30-60fb<sup>-1</sup>: 10 **IO\_1**  $5\sigma$  discovery H/A $\rightarrow \tau\tau$ 100 200 300 400 500 600 700 800 900 1000 (2007 analysis: arXiv:0704.0619)  $M_{A}$  [GeV/c<sup>2</sup>]

![](_page_34_Figure_0.jpeg)

## $B_{s,d} \rightarrow \mu^+ \mu^-$ as probe for New Physics

• <u>Example: MSSM</u> (with R-parity conservation)

$$BR(B_S \rightarrow \mu^+ \mu^-) \propto \frac{\tan^6 \beta}{m_A^4}$$

![](_page_34_Figure_4.jpeg)

→ limit or measurement of  $B_{s,d}$ →µµ s<sup>-</sup> will strongly constrain tanβ vs M<sub>A</sub> plane

### • <u>NUHM1</u>

Best fit contours in tanβ vs M<sub>A</sub> plane in the NUHM1 model [0. Buchmuller et al, arxiv:0907.5568] Regions compatible with

 $BR(B_s \rightarrow \mu\mu) = 2x10^{-8}, 1x10^{-8}, 5x10^{-9} \text{ and } SM$ 

LHCb calculation using F. Mahmoudi, Superlso, arXiv: 08083144

#### $\tan\beta$ vs M<sub>A</sub> plane

![](_page_34_Figure_11.jpeg)

![](_page_35_Picture_0.jpeg)

### Experimental status before summer 2011

![](_page_35_Figure_2.jpeg)

![](_page_36_Picture_0.jpeg)

### CDF "evidence"

#### Search for $B_s^0 \to \mu^+ \mu^-$ and $B^0 \to \mu^+ \mu^-$ Decays with CDF II

A search has been performed for  $B_s^0 \to \mu^+ \mu^-$  and  $B^0 \to \mu^+ \mu^-$  decays using 7 fb<sup>-1</sup> of integrated luminosity collected by the CDF II detector at the Fermilab Tevatron collider. The observed number of  $B^0$  candidates is consistent with background-only expectations and yields an upper limit on the branching fraction of  $\mathcal{B}(B^0 \to \mu^+ \mu^-) < 6.0 \times 10^{-9}$  at 95% confidence level. We observe an excess of  $B_s^0$  candidates. The probability that the background processes alone could produce such an excess or larger is 0.27%. The probability that the combination of background and the expected standard model rate of  $B_s^0 \to \mu^+ \mu^-$  could produce such an excess or larger is 1.9%. These data are used to determine  $\mathcal{B}(B_s^0 \to \mu^+ \mu^-) = (1.8^{+1.1}_{-0.9}) \times 10^{-8}$  and provide an upper limit of  $\mathcal{B}(B_s^0 \to \mu^+ \mu^-) < 4.0 \times 10^{-8}$  at 95% confidence level.

## arXiv: 1107.2304 [hep-ex]

12. July 2011

![](_page_36_Picture_8.jpeg)

![](_page_37_Picture_0.jpeg)

### CDF "evidence"

#### Search for $B_s^0 \to \mu^+ \mu^-$ and $B^0 \to \mu^+ \mu^-$ Decays with CDF II

M<sub>uu</sub> distribution in Bs search window for different NN bins

![](_page_37_Figure_4.jpeg)

2.8 σ assuming bkg-only hypothesis1.9% compatibility with bkg+SM hypothesis

 $0.46 \ge 10^{-8} \le BR \le 3.9 \ge 10^{-8}$  @ 90% CL (BR=1.8<sup>+1.1</sup>-0.9)  $\ge 10^{-8}$ 

![](_page_38_Picture_0.jpeg)

## $B_{s,d} \rightarrow \mu^+ \mu^-$ peak hunting I

Search for  $B_s^0 \to \mu^+ \mu^-$  and  $B^0 \to \mu^+ \mu^-$  Decays with CDF II

![](_page_38_Picture_3.jpeg)

![](_page_38_Picture_6.jpeg)

![](_page_39_Picture_0.jpeg)

### Selection

- Muon based triggers
- Soft selection to reduce size of dataset
- Similar to control channels

### Signal and background likelihoods

- Geometrical Likelihood (BDT)
   Multivariate classifier combining topological and kinematic information
- Invariant mass

### Normalization

 Convert number of observed events in branching fraction by normalizing with channels of known BR

### Extraction of the limit

Extract observation / exclusion measurement using the CL<sub>S</sub> method

![](_page_39_Figure_12.jpeg)

![](_page_39_Picture_15.jpeg)

Use 9 input variables:

![](_page_40_Figure_1.jpeg)

- B isolation
- Polarization variable
- Minimum Pt of the muons
- Choice of variables to avoid correlation with invariant mass
- Optimization and training on MC, using  $B_s \rightarrow \mu^+ \mu^$ and bb $\rightarrow \mu \mu X$  background

![](_page_40_Figure_7.jpeg)

![](_page_40_Figure_8.jpeg)

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![](_page_40_Picture_11.jpeg)

![](_page_41_Picture_0.jpeg)

### Signal likelihood calibration

BDT

identical decay topology

- Use events triggered independent of signal (TIS) to avoid trigger bias
- Signal distribution in GL flat as expected from simulation

![](_page_41_Figure_6.jpeg)

![](_page_42_Picture_0.jpeg)

- Signal invariant mass modelled with a crystal ball
  - Resolution obtained from data:
    - Interpolation between dilepton resonances (J/ $\psi$ ,  $\psi$ (2S) and Y)
    - Cross checked with inclusive B→h<sup>+</sup>h<sup>'-</sup>
  - − Mean from exclusive  $B^0 \rightarrow K^+\pi^-$  and  $B_s \rightarrow K^+K^-$

![](_page_42_Figure_7.jpeg)

 $\sigma(B_s) = (24.6 \pm 0.2 \pm 1.0) \text{ MeV/c}^2$  $\sigma(B_d) = (24.3 \pm 0.2 \pm 1.0) \text{ MeV/c}^2$ 

![](_page_42_Picture_11.jpeg)

- Combinatorial background expectation extracted from a fit to the mass sidebands in bins of BDT
- Systematics evaluated using different fit functions and ranges

![](_page_43_Figure_2.jpeg)

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![](_page_44_Figure_0.jpeg)

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![](_page_44_Picture_3.jpeg)

![](_page_45_Figure_0.jpeg)

## Results: $B_s \rightarrow \mu^+ \mu^-$

# LHCb result in the B<sub>s</sub> mass window with 300 pb<sup>-1</sup> (preliminary)

![](_page_45_Figure_3.jpeg)

	BDT<0.25	0.25 <bdt<0.5< th=""><th>0.5<bdt<0.75< th=""><th>0.75<bdt< th=""></bdt<></th></bdt<0.75<></th></bdt<0.5<>	0.5 <bdt<0.75< th=""><th>0.75<bdt< th=""></bdt<></th></bdt<0.75<>	0.75 <bdt< th=""></bdt<>
Exp.combinatorial	2968 ± 69	25 ± 2.5	2.99 ± 0.89	0.66 ± 0.40
Exp. SM signal	1.26 ± 0.13	0.61 ± 0.06	0.67 ± 0.07	0.72 ± 0.07
Observed	2872	26	3	2

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![](_page_46_Picture_0.jpeg)

## "Perfect" $\underline{B}_{s} \xrightarrow{\mu^{+}} \mu^{\pm} \mu^{-}$ candidate

![](_page_46_Figure_2.jpeg)

![](_page_46_Picture_5.jpeg)

![](_page_47_Figure_0.jpeg)

$B_s \rightarrow \mu^+ \mu^-$	90% CL	95% CL
Expected limit (bkg only)	8 x 10 <sup>-9</sup>	10 x 10 <sup>-9</sup>
Expected limit(bkg+SM)	12 x 10 <sup>-9</sup>	15 x 10 <sup>-9</sup>
Observed limit	13 x 10 <sup>-9</sup>	16 x 10⁻ <sup>9</sup>
combination 2010+2011	12 x 10 <sup>-9</sup>	15 x 10 <sup>-9</sup>

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![](_page_48_Picture_0.jpeg)

### Results: $\overline{B_d} \rightarrow \mu^+ \mu^-$

LHCb result in the  $B_d$  mass window with 300 pb<sup>-1</sup> (preliminary)

![](_page_48_Figure_3.jpeg)

	BDT<0.25	0.25 <bdt<0.5< th=""><th>0.5<bdt<0.75< th=""><th>0.75<bdt< th=""></bdt<></th></bdt<0.75<></th></bdt<0.5<>	0.5 <bdt<0.75< th=""><th>0.75<bdt< th=""></bdt<></th></bdt<0.75<>	0.75 <bdt< th=""></bdt<>
Exp.combinatorial	3175 ± 72	26.6 ± 2.5	3.1 ± 0.8	0.7 ± 0.4
Exp. MisID	0.6± 0.1	0.6± 0.1	0.6± 0.1	0.6± 0.1
Observed	3025	31	5	4

![](_page_49_Figure_0.jpeg)

$B_d \rightarrow \mu^+ \mu^-$	90% CL	95% CL
Expected limit (bkg only)	2.4 x 10 <sup>-9</sup>	3.1 x 10 <sup>-9</sup>
Observed limit	4.2 x 10 <sup>-9</sup>	5.2 x 10 <sup>-9</sup>

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![](_page_50_Figure_0.jpeg)

- CMS limit with 1.18/fb very competitive with LHCb
- Results combined using LHCbs f<sub>d</sub>/f<sub>s</sub>
- Observed distribution agrees very well with bkg+SM

![](_page_50_Figure_5.jpeg)

$B_s \rightarrow \mu^+ \mu^-$ , 95% CL	LHCb	CMS	
Expected limit (bkg+SM)	15 x 10 <sup>-9</sup>	18 x 10 <sup>-9</sup>	
Observed limit	15 x 10 <sup>-9</sup>	19 x 10 <sup>-9</sup>	
Observed LHCb+CMS	11 x 10 <sup>-9</sup>		
	CMS-PAS-BPH-11-019 and LHCb-CONF-2011-0		

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![](_page_50_Picture_9.jpeg)

![](_page_51_Picture_0.jpeg)

# Maybe winter (conferences) is a better time for mountaineering...

![](_page_51_Picture_3.jpeg)

![](_page_51_Picture_4.jpeg)

![](_page_51_Picture_6.jpeg)

![](_page_52_Figure_0.jpeg)

### Prospects: $B_s \rightarrow \mu^+ \mu^-$

![](_page_52_Figure_2.jpeg)

With the data collected in 2011 we will be able to explore the region BR~ 6-8×10<sup>-9</sup> at 95% CL

![](_page_52_Picture_6.jpeg)

![](_page_53_Figure_0.jpeg)

- LHC and LHCb are running extremely well
  - LHCb is taking data at higher than design luminosity
  - LHCb has >1fb<sup>-1</sup> recorded, analyses shown with 0.3fb<sup>-1</sup>
- LHCb has contributed the worlds most precise results on
  - − Forward-backward asymmetry in  $B^0 \rightarrow K^* \mu^+ \mu^-$
  - Measurements of the Bs mixing phase  $\phi_s$
  - Limits on the rare decay  $B_s \rightarrow \mu^+ \mu^-$
  - And many more
- But no hint for New Physics yet...
  - .. we've just gotten started: plenty left on the shopping list
  - Increase precision over the next 5 years
  - New observables welcome

![](_page_54_Picture_0.jpeg)

![](_page_54_Picture_1.jpeg)

![](_page_54_Picture_2.jpeg)

![](_page_54_Picture_4.jpeg)

## $A_{SI}$ and the like-sign dimuon anomaly

- Measuring  $A_{Sl}$  on a pp collider is tough: Production asymmetries
- More so at LHCb because we're not symmetric
  - Can't count like-sign muons when one of them isn't in your acceptance

![](_page_55_Figure_4.jpeg)

- LHCb has two independent analyses investigating this
- Time integrated  $A_{Sl}$  in  $B_s^0 \rightarrow D_s^- X \mu^+ \nu_\mu$ 
  - Production asymmetry is washed out by fast  $B_s^0 - \overline{B}_s^0$  mixing
- Time dependent subtraction:
  - $\blacktriangleright \Delta A_{fs}^{s,d} = A_{fs}^s A_{fs}^d$
  - ►  $B_s^0 \rightarrow D_s^- X \mu^+ \nu_\mu$  and
  - B → D<sup>-</sup> $X\mu^+\nu_\mu$  channels ► Production asymmetries cancel out
- The time-dependent analysis benefits from fewer systematics and cancellation of cross-feed backgrounds, while the time-integrated analysis benefits from fewer parameters to constrain
- Both analyses are progressing and can expect preliminary results soon.

![](_page_55_Picture_17.jpeg)

- Radiative  $b \rightarrow s$  penguin decay,  $B^0 \rightarrow K^* \gamma$  first seen by CLEO in 1993.
- Broader signal peak (compared to all-charged final states) implies more work on backgrounds  $(B^0 \rightarrow K^+\pi^-\pi^0, B_s \rightarrow K^+\pi^-\pi^0, B^0 \rightarrow K^{*0}e^+e^-, B_s \rightarrow K^+\pi^-\gamma)$  and cross-feed
- Simultaneous fit to  $B_s \rightarrow \varphi \gamma$  and  $B^0 \rightarrow K^* \gamma$ ;
  - mass difference fixed to PDG
- Largest  $B_s \rightarrow \varphi \gamma$  signal, measure:

 $\frac{\mathcal{B}(B^0 \to K^{*0} \gamma)}{\mathcal{B}(B^0_s \to \phi \gamma)} = 1.52 \pm 0.15 \text{(stat)} \pm 0.10 \text{(syst)} \pm 0.12 (f_s/f_d)$ 

• SCET predicts 1.0 ± 0.2 for this ratio [Ali et al., EPJ C55:577 (2008)]

![](_page_56_Figure_8.jpeg)

• Future steps: measure CP asymmetries

 $V_{tb} = W^- = V_{ts}$ 

![](_page_57_Figure_0.jpeg)

including S-wave: from 6 to 10 terms in angular/time distributions

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$ \begin{split} \frac{k}{1} & \frac{h_{k}(i)}{ A_{l} ^{2}(i) } & \frac{f_{k}(0,\psi,\psi)}{ 1-\sin^{2}\theta\cos^{2}\phi } \\ \frac{1}{2} &  A_{l}(i) ^{2} & \sin^{2}\psi(1-\sin^{2}\theta\cos^{2}\phi) \\ \frac{2}{3} &  A_{1}(i) ^{2} & \sin^{2}\psi(1-\sin^{2}\theta\cos^{2}\phi) \\ \frac{3}{3} &  A_{1}(i) ^{2} & \frac{1}{3}\sqrt{2}\sin^{2}\psi\sin^{2}\theta\sin^{2}\phi} \\ \frac{4}{3} & \Omega(A_{l}(i)A_{\perp}(i)) & \frac{1}{2}\sqrt{2}\sin^{2}\psi\sin^{2}\theta\sin^{2}\phi} \\ \frac{4}{3} & \Omega(A_{l}(i)A_{\perp}(i)) & \frac{1}{2}\sqrt{2}\sin^{2}\psi\sin^{2}\theta\sin^{2}\phi} \\ \frac{7}{3} &  A_{L}(i) ^{2} & \frac{1}{2}\sqrt{2}\sin^{2}\psi\sin^{2}\theta\sin^{2}\phi} \\ \frac{7}{3} &  A_{L}(i) ^{2} & \frac{1}{2}\sqrt{2}\sin^{2}\psi\sin^{2}\theta\sin^{2}\phi} \\ \frac{7}{3} &  A_{L}(i)A_{\perp}(i)) & \frac{1}{2}\sqrt{2}\sin^{2}\psi\sin^{2}\theta\cos^{2}\phi} \\ \frac{7}{3} &  A_{L}(i)A_{\perp}(i)) & \frac{1}{2}\sqrt{2}\sin^{2}\psi\sin^{2}\theta\cos^{2}\phi} \\ \frac{7}{3} &  A_{L}(i)A_{\perp}(i)) & \frac{1}{2}\sqrt{2}\sin^{2}\psi\sin^{2}\theta\sin^{2}\phi} \\ \frac{7}{3} &  A_{L}(i)A_{\perp}(i)) & \frac{1}{2}\sqrt{2}\sin^{2}\psi\sin^{2}\theta\cos^{2}\phi} \\ \frac{7}{3} &  A_{L}(i)A_{\perp}(i)) & \frac{1}{2}\sqrt{2}\sin^{2}\psi\sin^{2}\theta\sin^{2}\phi} \\ \frac{7}{3} &  A_{L}(i)A_{\perp}(i)) & \frac{1}{2}\sqrt{2}\cos^{2}\psi\sin^{2}\phi} \\ \frac{7}{3} &  A_{L}(i)A_{\perp}(i)  &  A_{\perp}(i)A_{\perp}(i)) & \frac{1}{2}\sqrt{2}\cos^{2}\psi\sin^{2}\phi} \\ \frac{1}{3} &  A_{\perp}(i)A_{\perp}(i)A_{\perp}(i)) & \frac{1}{2}\sqrt{2}\cos^{2}\psi\sin^{2}\phi} \\ \frac{1}{3} &  A_{\perp}(i)A_{\perp}(i)A_{\perp}(i)) & \frac{1}{2}\sqrt{2}\cos^{2}\psi\sin^{2}\phi} \\ \frac{1}{3} &  A_{\perp}(i)A_{\perp}(i)A_{\perp}(i)A_{\perp}(i)) & \frac{1}{2}\sqrt{2}\cos^{2}\psi\sin^{2}\phi} \\ \frac{1}{3} &  A_{\perp}(i)A_{\perp$								
$ \begin{vmatrix} 1 &   A_0 ^2(t) & 2\cos^2 \psi(1-\sin^2 \theta \cos^2 \psi) \\ \frac{2}{2} &   A_1(t) ^2 & \sin^2 \psi(1-\sin^2 \theta \sin^2 \psi) \\ \sin^2 \psi(1-\sin^2 \theta \sin^2 \psi) \\ \sin^2 \psi \sin^2 \theta \sin^2 \psi \\ \frac{2}{3} &   A_1(t) ^2 & \frac{1}{3}\sqrt{2}\sin^2 \theta \sin^2 \theta \sin^2 \psi \\ \frac{2}{3} &   A_1(t) ^2 & \frac{1}{2}\sqrt{2}\sin^2 \theta \sin^2 \theta \sin^2 \psi \\ \frac{2}{3} &   A_1(t) ^2 & \frac{1}{2}\sqrt{2}\sin^2 \theta \sin^2 \theta \cos^2 \psi \\ \hline 7 &   A_1(t) ^2 & \frac{1}{2}(1-\sin^2 \theta \cos^2 \psi) \\ \hline 7 &   A_1(t) ^2 & \frac{1}{2}(1-\sin^2 \theta \cos^2 \psi) \\ \hline 7 &   A_1(t) ^2 & \frac{1}{2}(1-\sin^2 \theta \cos^2 \psi) \\ \hline 8 & \mathbb{R}(A_{\bullet}^{\bullet}(1)A_1(t)) & \frac{1}{2}\sqrt{2}\sin^2 \theta \sin^2 \theta \sin^2 \theta \sin^2 \theta \sin^2 \theta \sin^2 \psi \\ \frac{9 & 0(A_{\bullet}^{\bullet}(1)A_1(t)) & \frac{1}{2}\sqrt{2}\sin^2 \theta \sin^2 \theta \cos^2 \psi \\ \hline 1 & \mathbb{R}(A_{\bullet}^{\bullet}(1)A_0(t)) & \frac{1}{2}\sqrt{2}\sin^2 \theta \sin^2 \theta \cos^2 \psi \\ \hline 1 & \mathbb{R}(A_{\bullet}^{\bullet}(1)A_0(t)) & \frac{1}{2}\sqrt{2}\sin^2 \theta \sin^2 \theta \cos^2 \psi \\ \hline 1 & \mathbb{R}(A_{\bullet}^{\bullet}(1)A_0(t)) & \frac{1}{2}\sqrt{2}\sin^2 \theta \sin^2 \theta \cos^2 \psi \\ \hline 1 & \mathbb{R}(A_{\bullet}^{\bullet}(1)A_0(t)) & \frac{1}{2}\sqrt{2}\sin^2 \theta \sin^2 \theta \sin^2 \theta \cos^2 \psi \\ \hline 1 & \mathbb{R}(A_{\bullet}^{\bullet}(1)A_0(t)) & \frac{1}{2}\sqrt{2}\sin^2 \theta \sin^2 \theta \sin^2 \theta \cos^2 \psi \\ \hline 1 & \mathbb{R}(A_{\bullet}^{\bullet}(1)A_0(t)) & \frac{1}{2}\sqrt{2}\sin^2 \theta \sin^2 \theta \sin^2 \theta \cos^2 \psi \\ \hline 1 & \mathbb{R}(A_{\bullet}^{\bullet}(1)A_0(t)) & \mathbb{R}(A_{\bullet}^{\bullet}(1)A_0(t)) & \frac{1}{2}\sqrt{2}\sin^2 \theta \sin^2 \theta \sin^2 \theta \cos^2 \psi \\ \hline \ A_0(t)\ ^2 &   A_0 ^2e^{-\Gamma_{\bullet\bullet}}[\cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\theta_{\bullet}\sinh\left(\frac{\Delta\Gamma}{2}t\right) + \sin\theta_{\bullet}\sin(\Delta m_0)],  (4) \\ \ A_1(t) ^2 &   A_1 ^2e^{-\Gamma_{\bullet\bullet}}[\cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\theta_{\bullet}\sinh\left(\frac{\Delta\Gamma}{2}t\right) + \sin\theta_{\bullet}\sin(\Delta m_0)],  (5) \\ \ A_1(t) ^2 &   A_1  ^2e^{-\Gamma_{\bullet\bullet}}[\cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\theta_{\bullet}\sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ & -\cos\theta_{\bullet} \sin(\Delta m_{0})],  (7) \\ \mathbb{R}(A_0(t)A_1(t)) &   A_0   A_1  e^{-\Gamma_{\bullet\bullet}}(-\cos\theta_{\bullet} - \delta_{0})\sinh\theta_{\bullet}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\theta_{\bullet}\sin(\Delta m_{0})],  (10) \\ \mathbb{R}(A_{\bullet}^{\bullet}(t)A_1(t)) &   A_0  A_1  e^{-\Gamma_{\bullet}}[-\sin(\theta_{\bullet} - \delta_{0})\cosh\theta_{\bullet}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\theta_{\bullet}\sin(\Delta m_{0})],  (10) \\ \mathbb{R}(A_{\bullet}^{\bullet}(t)A_1(t)) &   A_0  A_1  e^{-\Gamma_{\bullet}}[-\sin(\theta_{\bullet} - \delta_{0})\sinh\theta_{\bullet}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\theta_{\bullet}\sin(\Delta m_{0})],  (10) \\ \mathbb{R}(A_{\bullet}^{\bullet}(t)A_1(t)) &   A_0  A_1  e^{-\Gamma_{\bullet}}[-\sin(\theta_{\bullet} - \delta_{0})\cosh\theta_{\bullet}(\Delta\Gamma}{2}t) - \sin\theta_{\bullet}\sin(\Delta m_{0})],  (11) \\ \mathbb{Q}(A_{\bullet}^{\bullet}(t)A_1(t)) &   A_0  A_0  e^{-\Gamma_{\bullet}}[-\sin(\theta_{\bullet} - \delta_{0})\cosh\theta_{\bullet}(\Delta\Gamma}{2}t) - \sin\theta_{\bullet}\sin(\Delta m_{0})],  (11) \\ \mathbb{Q}(A_{\bullet}^{\bullet}(t)A_1(t)) &   A_0  A_0  e^{-\Gamma_{\bullet}}[-\sin(\theta_{\bullet} - \delta_{0})\cosh\theta_{\bullet}(\Delta\Gamma}{2}t) - \sin\theta_{$				k	$h_k(t)$	$f_k(\theta, \psi, \varphi)$		
$ \begin{vmatrix} 2 &  A_{1}(t) ^{2} & \sin^{2}\psi (1 - \sin^{2}\theta)^{2} \theta \\ 4 & \Im(A_{1}(t))^{2} & \sin^{2}\psi \sin^{2}\theta \\ - \sin^{2}\psi \sin^{2}\theta \sin^{2}\theta \\ 5 & \Re(A_{0}(t)A_{1}(t)) & \frac{1}{2}\sqrt{2}\sin^{2}\psi \sin^{2}\theta \sin^{2}\theta \\ 6 & \Im(A_{0}(t)A_{1}(t)) & \frac{1}{2}\sqrt{2}\sin^{2}\psi \sin^{2}\theta \sin^{2}\theta \\ 6 & \Im(A_{0}(t)A_{1}(t)) & \frac{1}{2}\sqrt{2}\sin^{2}\theta \cos^{2}\theta \\ 8 & \Re(A_{0}^{*}(t)A_{1}(t)) & \frac{1}{2}\sqrt{2}\sin^{2}\theta \cos^{2}\theta \\ 9 & \Im(A_{1}^{*}(t)A_{1}(t)) & \frac{1}{2}\sqrt{2}\sin^{2}\theta \sin^{2}\theta \cos^{2}\phi \\ 10 & \Re(A_{1}^{*}(t)A_{1}(t)) & \frac{1}{2}\sqrt{2}\sin^{2}\theta \sin^{2}\theta \sin^{2}\theta \sin^{2}\phi \\ 10 & \Re(A_{1}^{*}(t)A_{1}(t)) & \frac{1}{2}\sqrt{2}\sin^{2}\theta \sin^{2}\theta \sin^{2}\theta \sin^{2}\phi \\ 10 & \Re(A_{1}^{*}(t)A_{1}(t)) & \frac{1}{2}\sqrt{2}\sin^{2}\theta \sin^{2}\theta \sin^{2}\theta \sin^{2}\theta \sin^{2}\phi \\ 10 & \Re(A_{1}^{*}(t)A_{1}(t)) & -  A_{1} ^{2}e^{-\Gamma_{4}} \cosh\left(\frac{\Delta\Gamma_{1}}{2}\right) - \cos\phi_{4}\sinh\left(\frac{\Delta\Gamma_{1}}{2}\right) + \sin\phi_{4}\sin(\Delta\pi\omega) ,  (6) \\  A_{1}(t) ^{2} & -  A_{1} ^{2}e^{-\Gamma_{4}} \cosh\left(\frac{\Delta\Gamma_{1}}{2}\right) + \cos\phi_{4}\sinh\left(\frac{\Delta\Gamma_{1}}{2}\right) - \sin\phi_{4}\sin(\Delta\pi\omega) ,  (7) \\ \Re(A_{1}(t)A_{1}(t)) & -  A_{1}  A_{1} e^{-\Gamma_{4}^{*}} \cos\theta(A_{1}A_{1}) + \sin(\delta_{1} - \delta_{1})\cos(\Delta\pi\omega) ,  (7) \\ \Re(A_{0}(t)A_{1}(t)) & -  A_{0}  A_{1} e^{-\Gamma_{4}^{*}} \cos(\delta_{1} - \delta_{0}) \sin\phi_{4}\sinh\left(\frac{\Delta\Gamma_{1}}{2}\right) - \sin\phi_{4}\sin(\Delta\pi\omega) ,  (10) \\ \Re(A_{1}(t)A_{1}(t)) & -  A_{0}  A_{1} e^{-\Gamma_{4}^{*}} \cos(\Delta\Omega_{1}A_{1}) + \sin(\delta_{1} - \delta_{0})\cos(\Delta\pi\omega) ,  (11) \\ \Re(A_{1}^{*}(t)A_{1}(t)) & -  A_{1}  A_{1} e^{-\Gamma_{4}^{*}} \cos(\Delta\Omega_{1} - \delta_{0})\sin\phi_{4}\sinh\left(\frac{\Delta\Gamma_{1}}{2}\right) - \sin(\delta_{1} - \delta_{3})\cos\phi_{4}\sin(\Delta\pi\omega) ,  (12) \\ \Re(A_{1}^{*}(t)A_{1}(t)) & -  A_{1}  A_{1} e^{-\Gamma_{4}^{*}} \cos(\Delta\Omega_{1} - \delta_{1})\sin\phi_{4}\sinh\left(\frac{\Delta\Gamma_{1}}{2}t\right) - \sin(\delta_{1} - \delta_{3})\cos\phi_{4}\sin(\Delta\pi\omega) ,  (12) \\ \Re(A_{1}^{*}(t)A_{1}(t)) & -  A_{1}  A_{1} e^{-\Gamma_{4}^{*}} \sin(\delta_{1} - \delta_{3})\cos\phi_{4}\sin(\Delta\omega) ,  (13) \\ \Re(A_{1}^{*}(t)A_{1}(t)) & -  A_{1}  A_{1} e^{-\Gamma_{4}^{*}} \cos(\Delta\Omega_{1} - \delta_{3})\cos\phi_{4}\sin\omega  $				1	$ A_0 ^2(t)$	$2\cos^2\psi(1-\sin^2\theta\cos^2\phi)$		
$\begin{vmatrix} \mathbf{s} &  A_{\perp}(t) ^{2} & \sin^{2}\psi \sin^{2}\theta \\ -\sin^{2}\psi \sin^{2}\psi \sin^{2}\theta \\ -\sin^{2}\psi \sin^{2}\theta \\ -\sin^{2}\psi \sin^{2}\theta \\ -\sin^{2}\psi \sin^{2}\theta \\ -\sin^{2}\psi \\ -\sin^{2}\psi$				2	$ A_{\parallel}(t) ^2$	$\sin^2\psi \left(1-\sin^2\theta\sin^2\phi\right)$		
$ \begin{vmatrix} 4 & \Im(A_{1}(1), A_{1}(1)) & -\pi in^{2}\psi \sin 2\theta \sin \phi \\ \frac{5}{8} & \Re(A_{0}(1)A_{1}(1)) & \frac{1}{2}\sqrt{2} \sin 2\psi \sin^{2}\theta \sin 2\phi \\ \frac{6}{9} & \Im(A_{0}(1)A_{1}(1)) & \frac{1}{2}\sqrt{2} \sin 2\psi \sin^{2}\theta \cos \phi \\ \frac{7}{8} & \Re(A_{0}^{*}(1)A_{1}(1)) & \frac{1}{2}\sqrt{5} \sin \psi \sin^{2}\theta \cos \phi \\ \frac{9}{9} & \Im(A_{0}^{*}(1)A_{1}(1)) & \frac{1}{2}\sqrt{5} \sin \psi \sin^{2}\theta \cos \phi \\ \frac{9}{9} & \Im(A_{0}^{*}(1)A_{0}(1)) & \frac{1}{2}\sqrt{5} \sin \psi \sin^{2}\theta \cos \phi \\ \frac{9}{9} & \Im(A_{0}^{*}(1)A_{0}(1)) & \frac{1}{2}\sqrt{5} \sin \psi \sin^{2}\theta \cos \phi \\ \frac{9}{10} & \Re(A_{0}^{*}(1)A_{0}(1)) & \frac{1}{2}\sqrt{5} \sin \psi \sin^{2}\theta \cos \phi \\ \frac{9}{10} & \Re(A_{0}^{*}(1)A_{0}(1)) & \frac{1}{2}\sqrt{5} \sin \psi \sin^{2}\theta \cos^{2}\phi \\ \frac{1}{2} & \Re(A_{0}^{*}(1)A_{0}(1)) & \frac{1}{2}\sqrt{5} \sin \psi \sin^{2}\theta \cos^{2}\phi \\ \frac{1}{2} & \Re(A_{0}^{*}(1)A_{0}(1)) & \frac{1}{2}\sqrt{5} \sin \psi \sin^{2}\theta \cos^{2}\phi \\ \frac{1}{2} & \Re(A_{0}^{*}(1)A_{0}(1)) & \frac{1}{2}\sqrt{5} \sin \psi \sin^{2}\theta \cos^{2}\phi \\ \frac{1}{2} & \Re(A_{0}^{*}(1)A_{0}(1)) & \frac{1}{2}\sqrt{5} \sin \psi \sin^{2}\theta \cos^{2}\phi \\ \frac{1}{2} & \Re(A_{0}^{*}(1)A_{0}(1)) & \frac{1}{2}\sqrt{5} \sin^{2}\phi \sin^{2}(1) \\ \frac{1}{2}\sqrt{2} \sin^{2}\phi \sin$				3	$ A_{\perp}(t) ^{2}$	$s \ln^2 \psi s \ln^2 \theta$		
$ \begin{vmatrix} 5 & \Re(A_0(t)A_1(t)) & \frac{1}{2}\sqrt{2} \sin 2\psi \sin^2 \theta \tan 2\phi \\ \frac{1}{2}\sqrt{2} \sin 2\psi \sin^2 \theta \tan^2 \theta \\ \frac{1}{2}\sqrt{2} \sin 2\psi \sin^2 \theta \\ \frac{1}{2}\sqrt{2} \sin 2\psi \sin 2\theta \\ \frac{1}{2}\sqrt{2} \sin 2\psi \\ \frac{1}{2}\sqrt{2} \sin $				4	$\Im(A_{\parallel}(t) A_{\perp}(t))$	$-\sin^2\psi\sin 2\theta\sin\phi$		
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$				5	$\Re(A_0(t)A_{\parallel}(t))$	$\frac{1}{2}\sqrt{2} \sin 2\psi \sin^2 \theta \sin 2\phi$		
$\begin{bmatrix} 7 &  A_{n}(t) ^{2} & \frac{2}{3}(1 - \sin^{2}\theta \cos^{2}\phi) \\ \frac{1}{3}\sqrt{5}(3\pi\psi \sin^{2}\theta \sin^{2}\theta \sin^{2}\phi) \\ \frac{1}{3}\sqrt{5}\sin\psi \sin^{2}\theta \cos^{2}\phi) \\ \frac{1}{3}\sqrt{5}\sin\psi \sin^{2}\theta \cos^{2}\phi \\ \frac{1}{3}\sqrt{5}\sin^{2}\sin\psi \sin^{2}\theta \cos^{2}\phi \\ \frac{1}{3}\sqrt{5}\sin^{2}\sin\psi \sin^{2}\theta \cos^{2}\phi \\ \frac{1}{3}\sqrt{5}\sin^{2}\sin^{2}\theta \cos^{2}\phi \\ \frac{1}{3}\sqrt{5}\sin^{2}\theta \sin^{2}\phi \\ \frac{1}{3}\sqrt{5}\sin^{2}\theta \sin^{2}\theta \cos^{2}\phi \\ \frac{1}{3}\sqrt{5}\sin^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\phi \\ \frac{1}{3}\sqrt{5}\sin^{2}\theta \cos^{2}\phi \sin^{2}\theta \sin^{2}\theta \cos^{2}\phi \\ \frac{1}{3}\sqrt{5}\cos^{2}\theta \sin^{2}\theta \cos^{2}\phi \sin^{2}\theta \cos^{2}\phi \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \cos^{2}\theta \cos^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \cos^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \cos^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \cos^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \sin^{2}\theta \cos^{2}\theta \sin$				6	$\Im(A_0(t)A_{\perp}(t))$	$\frac{1}{2}\sqrt{2} \sin 2\psi \sin 2\theta \cos \phi$		
$ \begin{split} \left  \begin{array}{c} \frac{1}{9} \int_{\Omega} \langle \overline{Q}_{1}(t)A_{1}(t) \rangle \\ \frac{1}{9} \int_{\Omega} \langle \overline{Q}_{1}(t)A_{1}($				7	$ A_{s}(t) ^{2}$	$\frac{2}{3}(1 - \sin^2\theta \cos^2\phi)$		
$ \begin{array}{ c c c c c } \hline & \frac{1}{20} \sqrt{\frac{1}{8}(t_{*}^{*}(t)A_{\perp}(t))} & \frac{1}{2}\sqrt{\frac{1}{8} \operatorname{sch} \psi \sin 2\theta \cos \phi} \\ \hline & \frac{1}{20} & \frac{1}{8}(A_{*}^{*}(t)A_{0}(t)) & \frac{1}{4}\sqrt{\frac{1}{8} \operatorname{sch} \psi (1 - \sin^{2}\theta \cos^{2}\phi)} \end{array} \end{array} \\ \end{array} \\ The terms 7-10 are related to the description of the S-wave component, which has been added to this analysis. Expressed in terms of the size  A_{4}(0)  and phase \delta_{4} of the transversity and S-wave amplitudes at t = 0, the time dependent amplitudes are given by  A_{0} ^{2}(t) -  A_{0} ^{2}e^{-\Gamma_{*}t}[\cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_{*}\sinh\left(\frac{\Delta\Gamma}{2}t\right) + \sin\phi_{*}\sin(\Delta m t) , \qquad (4) \\  A_{1}(t) ^{2} -  A_{1} ^{2}e^{-\Gamma_{*}t}[\cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_{*}\sinh\left(\frac{\Delta\Gamma}{2}t\right) + \sin\phi_{*}\sin(\Delta m t) , \qquad (5) \\  A_{1}(t) ^{2} -  A_{1} ^{2}e^{-\Gamma_{*}t}[\cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_{*}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_{*}\sin(\Delta m t) , \qquad (6) \\ \Im(A_{1}(t)A_{\perp}(t)) -  A_{1}  A_{\perp} e^{-\Gamma_{*}t}[-\cos(\delta_{\perp} - \delta_{1})\sin\phi_{*}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_{*}\sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ -\cos(\delta_{\perp} - \delta_{1})\cos\phi_{*}\sin(\Delta m t) + \sin(\delta_{\perp} - \delta_{1})\cos(\Delta m t) , \qquad (7) \\ \Re(A_{0}(t)A_{1}(t)) -  A_{0}  A_{1} e^{-\Gamma_{*}t}[-\cos(\delta_{\perp} - \delta_{0})\sin\phi_{*}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_{*}\sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ -\cos(\delta_{\perp} - \delta_{0})\cos\phi_{*}\sin(\Delta m t) + \sin(\delta_{\perp} - \delta_{1})\cos(\Delta m t) , \qquad (9) \\  A_{*}(t) ^{2} -  A_{*} ^{2}e^{-\Gamma_{*}t}[\cosh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\phi_{*}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_{*}\sin(\Delta m t), \qquad (10) \\ \Re(A_{0}(t)A_{1}(t)) -  A_{0}  A_{1} e^{-\Gamma_{*}t}  - \sin(\delta_{1} - \delta_{*})\sin\phi_{*}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_{*}\sin(\Delta m t), \qquad (10) \\ \Re(A_{*}(t)A_{1}(t)) -  A_{*}  A_{1} e^{-\Gamma_{*}t}  - \sin(\delta_{1} - \delta_{*})\sin\phi_{*}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_{*}\sin(\Delta m t), \qquad (11) \\ \Re(A_{*}^{*}(t)A_{1}(t)) -  A_{*}  A_{1} e^{-\Gamma_{*}t}  - \sin(\delta_{1} - \delta_{*})\sin\phi_{*}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_{*}\sin(\Delta m t), \qquad (11) \\ \Re(A_{*}^{*}(t)A_{1}(t)) -  A_{*}  A_{1} e^{-\Gamma_{*}t}  - \sin(\delta_{1} - \delta_{*})\sin\phi_{*}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_{*}\sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ - \sin\phi_{*}\sin(\Delta m t)], \qquad (12) \\ \end{array}$				8	$\Re(A_{s}^{*}(t)A_{\parallel}(t))$	$\frac{1}{3}\sqrt{6}\sin\psi\sin^2\theta\sin 2\phi$		
$\frac{10}{\Re(A_{s}^{*}(t)A_{0}(t))} + \frac{1}{2}\sqrt{3} \operatorname{cosw}(1 - \sin^{2}\theta \cos^{2}\theta)$ The terms 7-10 are related to the description of the S-wave component, which has been added to this analysis. Expressed in terms of the size $ A_{t}(0) $ and phase $\delta_{t}$ of the transversity and S-wave amplitudes at $t = 0$ , the time dependent amplitudes are given by $ A_{0} ^{2}(t) -  A_{0} ^{2}e^{-\Gamma_{s}t} \cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_{s}\sinh\left(\frac{\Delta\Gamma}{2}t\right) + \sin\phi_{s}\sin(\Delta\pi\omega) ,  (4)$ $ A_{1}(t) ^{2} -  A_{1} ^{2}e^{-\Gamma_{s}t} \cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_{s}\sinh\left(\frac{\Delta\Gamma}{2}t\right) + \sin\phi_{s}\sin(\Delta\pi\omega) ,  (5)$ $ A_{1}(t) ^{2} -  A_{1} ^{2}e^{-\Gamma_{s}t} \cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_{s}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_{s}\sin(\Delta\pi\omega) ,  (6)$ $\Im(A_{1}(t)A_{1}(t)) -  A_{1}  A_{1} e^{-\Gamma_{s}t}  - \cos(\delta_{1} - \delta_{1})\sin\phi_{s}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_{s}\sin(\Delta\pi\omega) ,  (7)$ $\Re(A_{0}(t)A_{1}(t)) -  A_{0}  A_{1} e^{-\Gamma_{s}t}  - \cos(\delta_{1} - \delta_{0})\sin\phi_{s}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_{s}\sin(\Delta\pi\omega) ,  (9)$ $\frac{\Im(A_{0}(t)A_{1}(t)) -  A_{0}  A_{1} e^{-\Gamma_{s}t}  - \cos(\delta_{1} - \delta_{0})\sin\phi_{s}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_{s}\sin(\Delta\pi\omega) ,  (9)$ $\frac{\Im(A_{0}(t)A_{1}(t)) -  A_{0}  A_{1} e^{-\Gamma_{s}t}  - \cos(\delta_{1} - \delta_{0})\sin\phi_{s}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_{s}\sin(\Delta\pi\omega) ,  (9)$ $\frac{\Im(A_{0}(t)A_{1}(t)) -  A_{1}  A_{1} e^{-\Gamma_{s}t}  - \cos(\delta_{1} - \delta_{0})\sin\phi_{s}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_{s}\sin(\Delta\pi\omega) ,  (10)$ $\frac{\Re(A_{s}^{*}(t)A_{1}(t)) -  A_{s}  A_{1} e^{-\Gamma_{s}t}  - \sin(\delta_{1} - \delta_{s})\sin\phi_{s}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_{s}\sin(\Delta\pi\omega) ,  (11)$ $\frac{\Re(A_{s}^{*}(t)A_{1}(t)) -  A_{s}  A_{1} e^{-\Gamma_{s}t}  - \sin(\delta_{1} - \delta_{s})\sin\phi_{s}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_{s}\sin(\Delta\pi\omega) ,  (11)$ $\frac{\Re(A_{s}^{*}(t)A_{1}(t)) -  A_{s}  A_{1} e^{-\Gamma_{s}t}  - \sin(\delta_{1} - \delta_{s})\sin\phi_{s}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_{s}\sin(\Delta\pi\omega) ,  (11)$ $\frac{\Re(A_{s}^{*}(t)A_{1}(t)) -  A_{s}  A_{1} e^{-\Gamma_{s}t}  - \sin(\delta_{1} - \delta_{s})\sin\phi_{s}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_{s}\sin(\Delta\pi\omega) ,  (12)$ $\frac{\Re(A_{s}^{*}(t)A_{0}(t)) -  A_{s}  A_{0} e^{-\Gamma_{s}t}  - \sin(\delta_{1} - \delta_{s})\sin\phi_{s}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_{s}\sin(\Delta\pi\omega) ,  (12)$				9	$\Im(A_s^*(t)A_{\perp}(t))$	$\frac{1}{3}\sqrt{6}\sin\psi\sin 2\theta\cos\phi$		
The terms 7–10 are related to the description of the S-wave component, which has been added to this analysis. Expressed in terms of the size $ A_t(0) $ and phase $\delta_t$ of the transversity and S-wave amplitudes at $t = 0$ , the time dependent amplitudes are given by $ A_0 ^2(t) =  A_0 ^2 e^{-\Gamma_* t} [\cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) + \sin\phi_s \sin(\Delta m t) ,  (4)$ $ A_1(t) ^2 =  A_1 ^2 e^{-\Gamma_* t} [\cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) + \sin\phi_s \sin(\Delta m t) ,  (5)$ $ A_1(t) ^2 =  A_1 ^2 e^{-\Gamma_* t} [\cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta m t) ,  (5)$ $ A_1(t) ^2 =  A_1 ^2 e^{-\Gamma_* t} [\cosh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta m t) ,  (7)$ $\Re(A_0(t)A_1(t)) =  A_1  A_1 e^{-\Gamma_* t}(-\cos(\delta_1 - \delta_0)) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) + \sin\phi_s \sin(\Delta m t) ,  (7)$ $\Re(A_0(t)A_1(t)) =  A_0  A_1 e^{-\Gamma_* t} \cos(\delta_1 - \delta_0) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) + \sin\phi_s \sin(\Delta m t) ,  (9)$ $ A_s(t) ^2 =  A_s ^2 e^{-\Gamma_* t} [\cosh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta m t) ,  (10)$ $\Re(A_s(t)A_1(t)) =  A_s  A_1 e^{-\Gamma_* t}  -\sin(\delta_1 - \delta_s) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta m t) ,  (10)$ $\Re(A_s(t)A_1(t)) =  A_s  A_1 e^{-\Gamma_* t}  -\sin(\delta_1 - \delta_s) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta m t) ,  (10)$ $\Re(A_s(t)A_1(t)) =  A_s  A_1 e^{-\Gamma_* t}  -\sin(\delta_1 - \delta_s) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta m t) ,  (10)$ $\Re(A_s(t)A_1(t)) =  A_s  A_1 e^{-\Gamma_* t}  -\sin(\delta_1 - \delta_s) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta m t) ,  (11)$ $\Re(A_s(t)A_1(t)) =  A_s  A_1 e^{-\Gamma_* t}  -\sin(\delta_1 - \delta_s) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta m t) ,  (11)$ $\Re(A_s(t)A_1(t)) =  A_s  A_1 e^{-\Gamma_* t}  -\sin(\delta_1 - \delta_s) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta m t) ,  (11)$ $\Re(A_s(t)A_1(t)) =  A_s  A_1 e^{-\Gamma_* t}  -\sin(\delta_1 - \delta_s) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta m t) ,  (12)$ $\Re(A_s(t)A_1(t)) =  A_s  A_1 e^{-\Gamma_* t}  -\sin(\delta_1 - \delta_s) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta m t) ,  (12)$ $\Re(A_s(t)A_1(t)) =  A_s  A_1 e^{-\Gamma_* t}  -\sin(\delta_1 - \delta_s) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta m t) ,  (12)$				10	$\Re(A_{s}^{*}(t)A_{0}(t))$	$\frac{4}{3}\sqrt{3}\cos\psi(1-\sin^2\theta\cos^2\phi)$		
$\begin{split}  A_0 ^2(\mathbf{t}) &=  A_0 ^2 e^{-\Gamma_* \mathbf{t}} [\cosh\left(\frac{\Delta\Gamma}{2}\mathbf{t}\right) - \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}\mathbf{t}\right) + \sin\phi_s \sin(\Delta m u)],  (4) \\  A_{\parallel}(\mathbf{t}) ^2 &=  A_{\parallel} ^2 e^{-\Gamma_* \mathbf{t}} [\cosh\left(\frac{\Delta\Gamma}{2}\mathbf{t}\right) - \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}\mathbf{t}\right) + \sin\phi_s \sin(\Delta m u)],  (5) \\  A_{\perp}(\mathbf{t}) ^2 &=  A_{\perp} ^2 e^{-\Gamma_* \mathbf{t}} [\cosh\left(\frac{\Delta\Gamma}{2}\mathbf{t}\right) + \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}\mathbf{t}\right) - \sin\phi_s \sin(\Delta m u)],  (6) \\ \Im(A_{\parallel}(\mathbf{t})A_{\perp}(\mathbf{t})) &=  A_{\parallel}  A_{\perp} e^{-\Gamma_* \mathbf{t}}  - \cos(\delta_{\perp} - \delta_{\parallel}) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}\mathbf{t}\right) \\ &- \cos(\delta_{\perp} - \delta_{\parallel}) \cos\phi_s \sin(\Delta m u) + \sin(\delta_{\perp} - \delta_{\parallel}) \cos(\Delta m u)],  (7) \\ \Re(A_0(\mathbf{t})A_{\parallel}(\mathbf{t})) &=  A_0  A_{\parallel} e^{-\Gamma_* \mathbf{t}} \cos(\delta_{\parallel} - \delta_{\parallel}) \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}\mathbf{t}\right) \\ &+ \sin\phi_s \sin(\Delta m u)],  (8) \\ \\ \Im(A_0(\mathbf{t})A_{\perp}(\mathbf{t})) &=  A_0  A_{\perp} e^{-\Gamma_* \mathbf{t}} \cos(\delta_{\perp} - \delta_{\parallel}) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}\mathbf{t}\right) \\ &- \cos(\delta_{\perp} - \delta_{\parallel}) \cos\phi_s \sin(\Delta m u) + \sin(\delta_{\perp} - \delta_{\parallel}) \cos(\Delta m u)],  (10) \\ \Re(A_0(\mathbf{t})A_{\perp}(\mathbf{t})) &=  A_0  A_{\parallel} e^{-\Gamma_* \mathbf{t}} [-\sin(\delta_{\parallel} - \delta_{\parallel}) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}\mathbf{t}\right) \\ &- \cos(\delta_{\perp} - \delta_{\parallel}) \cos\phi_s \sin(\Delta m u) + \sin(\delta_{\perp} - \delta_{\parallel}) \cos(\Delta m u)],  (10) \\ \Re(A_s(\mathbf{t}) ^2 &=  A_s  A_{\parallel} e^{-\Gamma_* \mathbf{t}} [-\sin(\delta_{\parallel} - \delta_{\parallel}) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}\mathbf{t}\right) \\ &+ \cos(\delta_{\parallel} - \delta_{\parallel}) \sin\phi_s \sin\left(\frac{\Delta\Gamma}{2}\mathbf{t}\right) \\ &+ \cos(\delta_{\parallel} - \delta_{\parallel}) \sin\phi_s \sin\left(\frac{\Delta\Gamma}{2}\mathbf{t}\right) \\ &+ \cos(\delta_{\parallel} - \delta_{\parallel}) \sin\phi_s \sin\left(\frac{\Delta\Gamma}{2}\mathbf{t}\right) \\ &- \sin\phi_s \sin(\Delta m u)],  (11) \\ \Im(A_s(\mathbf{t})A_{\perp}(\mathbf{t})) &=  A_s  A_{\parallel} e^{-\Gamma_* \mathbf{t}} [-\sin(\delta_{\parallel} - \delta_{\parallel}) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}\mathbf{t}\right) \\ &- \sin\phi_s \sin(\Delta m u)],  (11) \\ \Im(A_s(\mathbf{t})A_{\perp}(\mathbf{t})) &=  A_s  A_{\parallel} e^{-\Gamma_* \mathbf{t}} [-\sin(\delta_{\parallel} - \delta_{\parallel}) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}\mathbf{t}\right) \\ &- \sin\phi_s \sin(\Delta m u)],  (12) \\ \Re(A_s(\mathbf{t})A_{\perp}(\mathbf{t})) &=  A_s  A_{\parallel} e^{-\Gamma_* \mathbf{t}} [-\sin(\delta_{\parallel} - \delta_{\parallel}) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}\mathbf{t}\right) \\ &- \sin\phi_s \sin(\Delta m u)],  (12) \\ \Re(A_s(\mathbf{t})A_{\perp}(\mathbf{t})) &=  A_s  A_{\parallel} e^{-\Gamma_* \mathbf{t}} [-\sin(\delta_{\parallel} - \delta_{\parallel}) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}\mathbf{t}\right) \\ &- \sin\phi_s \sin(\Delta m u)],  (12) \\ \Re(A_s(\mathbf{t})A_{\perp}(\mathbf{t})) &=  A_s  A_{\parallel} e^{-\Gamma_* \mathbf{t}} [-\sin(\delta_{\parallel} - \delta_{\parallel}) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}\mathbf{t}\right) \\ &- \sin\phi_s \sin(\Delta m u)],  (12) \\ \Re(A_s(\mathbf{t})A_{\perp}(\mathbf{t})) &=  A_s  A_{\parallel} A_{\parallel} e^{-\Gamma_* \mathbf{t}} [-\sin(\delta_{\parallel} - \delta_{\parallel}) \sin\phi_s \sin(\Delta m t) + \sin(\delta_{\perp} - \delta_{\parallel}) \cos\phi_s \sin(\Delta m t) \\ \\ \Re(A_s(\mathbf{t})A_{\perp}(\mathbf{t})) &=  A_s  A_{\parallel} A_{\parallel} e^{-\Gamma_* \mathbf{t}} [-\sin(\delta_{$	The te added sity an	rms 7–10 are to this analys d S-wave am	rela sis. 1 plita	ated t Expre ides s	to the descript sed in terms at $t = 0$ , the t	tion of the S-wave com of the size $ A_t(0) $ and ime dependent amplitu	ponent, which has phase $\delta_i$ of the tran ides are given by	been nsver-
$\begin{split}  A_{\parallel}(t) ^2 &=  A_{\parallel} ^2 e^{-\Gamma_* t} [\cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) + \sin\phi_s \sin(\Delta m t)],  (5) \\  A_{\perp}(t) ^2 &=  A_{\perp} ^2 e^{-\Gamma_* t} [\cosh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta m t)],  (6) \\ \Im(A_{\parallel}(t)A_{\perp}(t)) &=  A_{\parallel}  A_{\perp} e^{-\Gamma_* t} [-\cos(\delta_{\perp} - \delta_{\parallel})\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &-\cos(\delta_{\perp} - \delta_{\parallel})\cos\phi_s \sin(\Delta m t) + \sin(\delta_{\perp} - \delta_{\parallel})\cos(\Delta m t)],  (7) \\ \Re(A_{0}(t)A_{\parallel}(t)) &=  A_{0}  A_{\parallel} e^{-\Gamma_* t} \cos(\delta_{\parallel} - \delta_{0})[\cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &+\sin\phi_s \sin(\Delta m t)],  (8) \\ \\ \Im(A_{0}(t)A_{\perp}(t)) &=  A_{0}  A_{\perp} e^{-\tau_* t} [-\cos(\delta_{\perp} - \delta_{0})\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &-\cos(\delta_{\perp} - \delta_{0})\cos\phi_s \sin(\Delta m t) + \sin(\delta_{\perp} - \delta_{0})\cos(\Delta m t)],  (9) \\ \\ \Im(A_{0}(t)A_{\perp}(t)) &=  A_{0}  A_{\perp} e^{-\tau_* t} [-\cos(\delta_{\perp} - \delta_{0})\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &-\cos(\delta_{\perp} - \delta_{0})\cos\phi_s \sin(\Delta m t) + \sin(\delta_{\perp} - \delta_{0})\cos(\Delta m t)],  (10) \\ \Re(A_{\bullet}^{*}(t)A_{\parallel}(t)) &=  A_{\bullet}  A_{\parallel} e^{-\Gamma_* t} [-\sin(\delta_{\parallel} - \delta_{\bullet})\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &+\cos(\delta_{\parallel} - \delta_{\bullet})\cos(\Delta m t)],  (11) \\ \Im(A_{\bullet}^{*}(t)A_{\perp}(t)) &=  A_{\bullet}  A_{\parallel} e^{-\Gamma_* t} [-\sin(\delta_{\parallel} - \delta_{\bullet})\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &-\sin\phi_s \sin(\Delta m t)],  (11) \\ \Im(A_{\bullet}^{*}(t)A_{\perp}(t)) &=  A_{\bullet}  A_{\parallel} e^{-\Gamma_* t} [-\sin(\delta_{\parallel} - \delta_{\bullet})\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &-\sin\phi_s \sin(\Delta m t)],  (12) \\ \Re(A_{\bullet}^{*}(t)A_{0}(t)) &=  A_{\bullet}  A_{\parallel} e^{-\Gamma_* t} [-\sin(\delta_{\parallel} - \delta_{\bullet})\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &-\sin\phi_s \sin(\Delta m t)],  (12) \\ \Re(A_{\bullet}^{*}(t)A_{0}(t)) &=  A_{\bullet}  A_{\parallel} e^{-\Gamma_* t} [-\sin(\delta_{\parallel} - \delta_{\bullet})\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &-\sin\phi_s \sin(\Delta m t)],  (12) \\ \Re(A_{\bullet}^{*}(t)A_{0}(t)) &=  A_{\bullet}  A_{\parallel} e^{-\Gamma_* t} [-\sin(\delta_{\parallel} - \delta_{\bullet})\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &-\sin(\delta_{\parallel} - \delta_{\bullet})\cos\phi_s \sin(\Delta m t) + \cos(\delta_{\parallel} - \delta_{\bullet})\cos(\Delta m t)].  (13) \end{aligned}$		$ A_0 ^2(t)$	-	$ A_0 ^2 e$	$-\Gamma_{s}t \left[ \cosh \left( \frac{\Delta \Gamma}{2} t \right) \right]$	$-\cos \phi_s \sinh \left(\frac{\Delta \Gamma}{2}t\right) + \sin \phi_s \sin \phi_s$	$n(\Delta mt)$ ],	(4)
$\begin{split}  A_{\perp}(t) ^2 &=  A_{\perp} ^2 e^{-\Gamma_{t}t} [\cosh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta mt) ,  (6) \\ \Im(A_{\parallel}(t)A_{\perp}(t)) &=  A_{\parallel}  A_{\perp} e^{-\Gamma_{t}t}  - \cos(\delta_{\perp} - \delta_{\parallel}) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ & -\cos(\delta_{\perp} - \delta_{\parallel}) \cos\phi_s \sin(\Delta mt) + \sin(\delta_{\perp} - \delta_{\parallel}) \cos(\Delta mt) ,  (7) \\ \Re(A_0(t)A_{\parallel}(t)) &=  A_0  A_{\parallel} e^{-\Gamma_{t}t} \cos(\delta_{\parallel} - \delta_{0}) [\cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ & +\sin\phi_s \sin(\Delta mt) ,  (8) \\ \\ \Im(A_0(t)A_{\perp}(t)) &=  A_0  A_{\perp} e^{-\tau_{t}t}  - \cos(\delta_{\perp} - \delta_{0}) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ & -\cos(\delta_{\perp} - \delta_{0}) \cos\phi_s \sin(\Delta mt) + \sin(\delta_{\perp} - \delta_{0}) \cos(\Delta mt) ,  (9) \\  A_s(t) ^2 &=  A_s ^2 e^{-\Gamma_{t}t} [\cosh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta mt), \\ & +\cos(\delta_{\parallel} - \delta_{s}) \cos\phi_s \sin(\Delta mt)],  (10) \\ \Re(A_s^*(t)A_{\parallel}(t)) &=  A_s  A_{\parallel} e^{-\Gamma_{t}t}  - \sin(\delta_{\parallel} - \delta_{s}) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin(\delta_{\parallel} - \delta_{s}) \cos\phi_s \sin(\Delta mt) \\ & +\cos(\delta_{\parallel} - \delta_{s}) \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ & -\sin\phi_s \sin(\Delta mt) ,  (11) \\ \Im(A_s^*(t)A_{\perp}(t)) &=  A_s  A_{\parallel} e^{-\Gamma_{t}t}  - \sin(\delta_{\parallel} - \delta_{s}) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ & -\sin\phi_s \sin(\Delta mt) ,  (12) \\ \Re(A_s^*(t)A_{\perp}(t)) &=  A_s  A_{\parallel} e^{-\Gamma_{t}t}  - \sin(\delta_{\parallel} - \delta_{s}) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ & -\sin\phi_s \sin(\Delta mt) ,  (12) \\ \Re(A_s^*(t)A_{\perp}(t)) &=  A_s  A_{\parallel} e^{-\Gamma_{t}t}  - \sin(\delta_{\parallel} - \delta_{s}) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ & -\sin\phi_s \sin(\Delta mt) ,  (12) \\ \Re(A_s^*(t)A_{\perp}(t)) &=  A_s  A_{\parallel} e^{-\Gamma_{t}t}  - \sin(\delta_{\parallel} - \delta_{s}) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ & -\sin\phi_s \sin(\Delta mt) ,  (12) \\ \Re(A_s^*(t)A_{\perp}(t)) &=  A_s  A_{\parallel} e^{-\Gamma_{t}t}  - \sin(\delta_{\parallel} - \delta_{s}) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ & -\sin\phi_s \sin(\Delta mt) ,  (12) \\ \Re(A_s^*(t)A_{\perp}(t)) &=  A_s  A_{\parallel} e^{-\Gamma_{t}t}  - \sin(\delta_{\parallel} - \delta_{s}) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ & -\sin\phi_s \sin(\Delta mt) ,  (13) \\ \Re(A_s^*(t)A_{\perp}(t)) &=  A_s  A_{\parallel} e^{-\Gamma_{t}t}  - \sin(\delta_{\parallel} - \delta_{s}) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ & -\sin(\delta_{\parallel} - \delta_{s}) \cos\phi_s \sin\left(\Delta mt\right) + \cos(\delta_{\parallel} - \delta_{s}) \cos\phi(\Delta mt) .  (13) \\ \Re(A_s^*(t)A_{\parallel}(t)) &=  A_s  A_{\parallel} A_{\parallel} E^{-\Gamma_{t}t}  - \sin(\delta_{\parallel} - \delta_{\parallel}) \sin\phi(\Delta mt) + \cos(\delta_{\parallel} - \delta_{\parallel}) \cos\phi(\Delta mt) .  (13) \\ \Re(A_s^*(t)A_{\parallel}(t)) &=  A_s  A_{\parallel} A_{\parallel} E^{-\Gamma_{t}t}  - \sin(\delta_{\parallel} - \delta_{\parallel}) \sin\phi(\Delta mt) + \cos(\delta_{\parallel} - \delta_{\parallel}) \cos\phi(\Delta mt) .  (13) \\ \Re(A_s^*(t)A_{\parallel}(t)) &=  A_s  A_{$		$ A_{\ }(t) ^{2}$	-	$ A_{\parallel} ^2 \epsilon$	$-\Gamma_{s}t \left[ \cosh\left(\frac{\Delta\Gamma}{2}t\right) \right]$	$-\cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) + \sin\phi_s \sin$	$n(\Delta mt)$ ],	(5)
$\begin{split} & \Im(A_{\parallel}(t)A_{\perp}(t)) =  A_{\parallel}  A_{\perp} e^{-\Gamma_{*}t}  - \cos(\delta_{\perp} - \delta_{\parallel})\sin\phi_{s}\sinh(\frac{\Delta\Gamma}{2}t) \\ & -\cos(\delta_{\perp} - \delta_{\parallel})\cos\phi_{s}\sin(\Delta m t) + \sin(\delta_{\perp} - \delta_{\parallel})\cos(\Delta m t) ,  (7) \\ & \Re(A_{0}(t)A_{\parallel}(t)) =  A_{0}  A_{\parallel} e^{-\Gamma_{*}t}\cos(\delta_{\parallel} - \delta_{0})[\cosh(\frac{\Delta\Gamma}{2}t) - \cos\phi_{s}\sinh(\frac{\Delta\Gamma}{2}t) \\ & +\sin\phi_{s}\sin(\Delta m t) ,  (8) \\ & \qquad \qquad$		$ A_{\perp}(t) ^2$	-	$ A_{\perp} ^2$	$t^{-\Gamma_{a}t} \left[ \cosh \left( \frac{\Delta \Gamma}{2} t \right) \right]$	$+\cos\phi_a \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_a \sin$	$in(\Delta mt)]$ ,	(6)
$-\cos(\delta_{\perp} - \delta_{\perp}])\cos\phi_s \sin(\Delta m t) + \sin(\delta_{\perp} - \delta_{\parallel})\cos(\Delta m t)],  (7)$ $\Re(A_0(t)A_{\parallel}(t)) =  A_0  A_{\parallel} e^{-\Gamma_s t}\cos(\delta_{\parallel} - \delta_0)]\cosh\left(\frac{\Delta \Gamma}{2}t\right) - \cos\phi_s \sinh\left(\frac{\Delta \Gamma}{2}t\right) \\ +\sin\phi_s \sin(\Delta m t)],  (8)$ $\frac{\Im(A_0(t)A_{\perp}(t)) =  A_0  A_{\perp} e^{-\tau_s t}] - \cos(\delta_{\perp} - \delta_0)\sin\phi_s \sinh\left(\frac{\Delta \Gamma}{2}t\right) \\ -\cos(\delta_{\perp} - \delta_0)\cos\phi_s \sin(\Delta m t) + \sin(\delta_{\perp} - \delta_0)\cos(\Delta m t)],  (9)$ $ A_s(t) ^2 =  A_s ^2 e^{-\Gamma_s t} [\cosh\left(\frac{\Delta \Gamma}{2}t\right) + \cos\phi_s \sinh\left(\frac{\Delta \Gamma}{2}t\right) - \sin\phi_s \sin(\Delta m t),  (10)$ $\Re(A_s(t)A_{\parallel}(t)) =  A_s  A_{\parallel} e^{-\Gamma_s t}  - \sin(\delta_{\parallel} - \delta_s)\sin\phi_s \sinh\left(\frac{\Delta \Gamma}{2}t\right) - \sin(\delta_{\parallel} - \delta_s)\cos\phi_s \sin(\Delta m t) \\ + \cos(\delta_{\parallel} - \delta_s)\cos(\Delta m t)],  (11)$ $\Im(A_s^*(t)A_{\perp}(t)) =  A_s  A_{\parallel} e^{-\Gamma_s t} \sin(\delta_{\perp} - \delta_s) \cosh\left(\frac{\Delta \Gamma}{2}t\right) + \cos\phi_s \sinh\left(\frac{\Delta \Gamma}{2}t\right) \\ - \sin\phi_s \sin(\Delta m t)],  (11)$ $\Re(A_s^*(t)A_{\perp}(t)) =  A_s  A_{\parallel} e^{-\Gamma_s t} \sin(\delta_{\perp} - \delta_s) \cosh\left(\frac{\Delta \Gamma}{2}t\right) + \cos\phi_s \sinh\left(\frac{\Delta \Gamma}{2}t\right) \\ - \sin\phi_s \sin(\Delta m t)],  (12)$ $\Re(A_s^*(t)A_{0}(t)) =  A_s  A_{\parallel} e^{-\Gamma_s t} = \sin(\delta_0 - \delta_s)\sin\phi_s \sinh\left(\frac{\Delta \Gamma}{2}t\right) \\ - \sin(\delta_0 - \delta_s)\cos\phi_s \sin(\Delta m t) + \cos(\delta_0 - \delta_s)\cos(\Delta m t)].  (13)$		$\Im(A_{\parallel}(t)A_{\perp}(t))$	-	A <sub>  </sub>   A	$_{\perp} e^{-\Gamma_{a}t} -\cos(\delta_{\perp}$	$-\delta_{\parallel}$ sin $\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right)$		
$\begin{split} \Re(A_0(t)A_{\parallel}(t)) &=  A_0  A_{\parallel} e^{-\Gamma_* t}\cos(\delta_{\parallel} - \delta_0) \cosh\left(\frac{\Delta\Gamma}{2}t\right) - \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &+ \sin\phi_s \sin(\Delta \pi u) , \end{split} \tag{8}$ $\begin{aligned} & \qquad $				- cos(e	$\delta_{\perp} = \delta_{\parallel} \cos \phi_s \sin \phi_s$	$(\Delta mt) + \sin(\delta_{\perp} - \delta_{\parallel}) \cos(\Delta mt)$	1,	(7)
$\begin{aligned} \Re(\iota_{0}(t)A_{\parallel}(t)) &=  \iota_{0} _{1}\Re[t^{-1} - \cos(\iota_{0} - \delta_{0})\sin(\iota_{2} t) - \cos(\iota_{2} t) + \sin(\iota_{2} t) \\ &+ \sin\phi_{s}\sin(\Delta m s) , \end{aligned} \tag{8} \\ & \qquad \qquad$		$\overline{W}(A_{n}(t) A_{n}(t))$	_	Ide IId	sla <sup>−Γ</sup> s <sup>‡</sup> cos(δ <sub>1</sub> − δ <sub>2</sub>	$V \cosh\left(\frac{\Delta\Gamma}{t}\right) = \cos\phi_{s} \sinh\left(\frac{\Delta\Gamma}{t}\right)$	Ar,	
$\frac{+ \sin \phi_s \sin (\Delta m c)]_{\tau}}{\Im (A_0(t) A_{\perp}(t))} = \frac{ A_0   A_{\perp}  e^{-t_x t}  -\cos(\delta_{\perp} - \delta_0) \sin \phi_s \sinh \left(\frac{\Delta t + 1}{2} t\right)}{-\cos(\delta_{\perp} - \delta_0) \cos(\phi_s \sin(\Delta m t) + \sin(\delta_{\perp} - \delta_0) \cos(\Delta m t)]_{\tau}} $ (9) $ A_s(t) ^2 =  A_s ^2 e^{-\Gamma_s t} [\cosh \left(\frac{\Delta \Gamma}{2} t\right) + \cos\phi_s \sinh \left(\frac{\Delta \Gamma}{2} t\right) - \sin\phi_s \sin(\Delta m t), $ (10) $\Re (A_s^*(t) A_{\parallel}(t)) =  A_s   A_{\parallel}  e^{-\Gamma_s t} [-\sin(\delta_{\parallel} - \delta_s) \sin\phi_s \sinh \left(\frac{\Delta \Gamma}{2} t\right) - \sin(\delta_{\parallel} - \delta_s) \cos\phi_s \sin(\Delta m t) + \cos(\delta_{\parallel} - \delta_s) \cos\phi_s \sin(\Delta m t)]_{\tau} $ (11) $\Im (A_s^*(t) A_{\perp}(t)) =  A_s   A_{\perp}  e^{-\Gamma_s t} \sin(\delta_{\perp} - \delta_s) [\cosh \left(\frac{\Delta \Gamma}{2} t\right) + \cos\phi_s \sinh \left(\frac{\Delta \Gamma}{2} t\right) - \sin(\delta_{\parallel} - \delta_s) \cos\phi_s \sin(\Delta m t) + \cos(\delta_{\parallel} - \delta_s) \cos\phi_s \sin(\Delta m t)]_{\tau} $ (12) $\Re (A_s^*(t) A_0(t)) =  A_s   A_0  e^{-\Gamma_s t} [-\sin(\delta_0 - \delta_s) \sin\phi_s \sinh \left(\frac{\Delta \Gamma}{2} t\right) - \sin(\delta_0 - \delta_s) \cos\phi_s \sin(\Delta m t) + \cos(\delta_0 - \delta_s) \cos(\Delta m t)]_{\tau} .$ (13)		a(au(e) a f(e))		paulla.	The control - of	Mean ( 2 ) - conder min (	2 *)	(
$\begin{aligned} & \Re(A_0(t)A_{\perp}(t)) &=  A_0  A_{\perp} e^{-\Gamma_* t}[-\cos(\delta_{\perp} - \delta_0)\sin\phi_s \sinh(\frac{1}{2}t) \\ & -\cos(\delta_{\perp} - \delta_0)\cos\phi_s \sin(\Delta m t) + \sin(\delta_{\perp} - \delta_0)\cos(\Delta m t)], \\ &  A_s(t) ^2 &=  A_s ^2 e^{-\Gamma_* t}[\cosh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin(\Delta m t), \\ & (10) \\ & \Re(A_s^*(t)A_{\parallel}(t)) &=  A_s  A_{\parallel} e^{-\Gamma_* t}[-\sin(\delta_{\parallel} - \delta_s)\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin(\delta_{\parallel} - \delta_s)\cos\phi_s \sin(\Delta m t) \\ & +\cos(\delta_{\parallel} - \delta_s)\cos(\Delta m t)], \\ & \Im(A_s^*(t)A_{\perp}(t)) &=  A_s  A_{\perp} e^{-\Gamma_* t}\sin(\delta_{\perp} - \delta_s)[\cosh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ & -\sin\phi_s \sin(\Delta m t)], \\ & \Re(A_s^*(t)A_{0}(t)) &=  A_s  A_{0} e^{-\Gamma_* t}[-\sin(\delta_{0} - \delta_s)\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ & -\sin(\delta_{0} - \delta_{s})\cos\phi_s \sin(\Delta m t) + \cos(\delta_{0} - \delta_s)\cos(\Delta m t)]. \end{aligned}$ (13)				+ sin ¢	$sin(\Delta mt)$ ,	(40)		(8)
$\begin{aligned} & -\cos(\delta_{\perp} - \delta_{0})\cos\varphi_{s}\sin(\Delta m i) + \sin(\delta_{\perp} - \delta_{0})\cos(\Delta m i)],  (9) \\ &  A_{s}(t) ^{2} = - A_{s} ^{2}e^{-\Gamma_{s}t}[\cosh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\varphi_{s}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\varphi_{s}\sin(\Delta m i),  (10) \\ & \Re(A_{s}^{*}(t)A_{\parallel}(t)) =  A_{s}  A_{\parallel} e^{-\Gamma_{s}t}[-\sin(\delta_{\parallel} - \delta_{s})\sin\varphi_{s}\sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin(\delta_{\parallel} - \delta_{s})\cos\varphi_{s}\sin(\Delta m i) \\ & +\cos(\delta_{\parallel} - \delta_{s})\cos(\Delta m i)],  (11) \\ & \Im(A_{s}^{*}(t)A_{\perp}(t)) =  A_{s}  A_{\perp} e^{-\Gamma_{s}t}\sin(\delta_{\perp} - \delta_{s}) \cosh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\varphi_{s}\sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ & -\sin\varphi_{s}\sin(\Delta m i)],  (12) \\ & \Re(A_{s}^{*}(t)A_{0}(t)) =  A_{s}  A_{0} e^{-\Gamma_{s}t}[-\sin(\delta_{0} - \delta_{s})\sin\varphi_{s}\sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ & -\sin(\delta_{0} - \delta_{s})\cos\varphi_{s}\sin(\Delta m t) + \cos(\delta_{0} - \delta_{s})\cos(\Delta m i)].  (13) \end{aligned}$		$\Im(A_0(t)A_\perp(t))$	-	A <sub>0</sub>   A	$T[e_{-,*}] = \cos(qT \cdot$	$-\delta_0 \sin \phi_s \sinh \left(\frac{1}{2}t\right)$		
$\begin{split}  A_s(t) ^2 &=  A_s ^2 e^{-\Gamma_s t} [\cosh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sinh(\Delta m t),  (10) \\ \Re(A_s^*(t)A_{\parallel}(t)) &=  A_s  A_{\parallel} e^{-\Gamma_s t} [-\sin(\delta_{\parallel} - \delta_s)\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin(\delta_{\parallel} - \delta_s)\cos\phi_s \sin(\Delta m t) \\ &+ \cos(\delta_{\parallel} - \delta_s)\cos\phi(\Delta m t)],  (11) \\ \Im(A_s^*(t)A_{\perp}(t)) &=  A_s  A_{\perp} e^{-\Gamma_s t} \sin(\delta_{\perp} - \delta_s) [\cosh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &- \sin\phi_s \sin(\Delta m t)],  (12) \\ \Re(A_s^*(t)A_{0}(t)) &=  A_s  A_{0} e^{-\Gamma_s t} [-\sin(\delta_{0} - \delta_s)\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &- \sin(\delta_{0} - \delta_s)\cos\phi_s \sin(\Delta m t) + \cos(\delta_{0} - \delta_s)\cos(\Delta m t)].  (13) \end{split}$				- cos(e	$\delta_{\perp} - \delta_0 \cos \phi_s \sin($	$\Delta mt$ ) + sin( $\delta_{\perp} - \delta_0$ ) cos( $\Delta mt$ )]	,	(9)
$\begin{aligned} & \Re(A_s^{\bullet}(t)A_{\parallel}(t)) &=  A_s  A_{\parallel} e^{-\Gamma_s t}[-\sin(\delta_{\parallel} - \delta_s)\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin(\delta_{\parallel} - \delta_s)\cos\phi_s \sin(\Delta m t) \\ &+ \cos(\delta_{\parallel} - \delta_s)\cos(\Delta m t)], \end{aligned} \tag{11} \\ & \Im(A_s^{\bullet}(t)A_{\perp}(t)) &=  A_s  A_{\perp} e^{-\Gamma_s t}\sin(\delta_{\perp} - \delta_s) \cosh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &- \sin\phi_s \sin(\Delta m t)], \end{aligned} \tag{12} \\ & \Re(A_s^{\bullet}(t)A_0(t)) &=  A_s  A_0 e^{-\Gamma_s t} -\sin(\delta_0 - \delta_s)\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &- \sin(\delta_0 - \delta_s)\cos\phi_s \sin(\Delta m t) + \cos(\delta_0 - \delta_s)\cos(\Delta m t)]. \end{aligned}$		$ A_s(t) ^2$	-	$ A_s ^2 c$	$-\Gamma_{st} \left[ \cosh \left( \frac{\Delta \Gamma}{2} t \right) \right]$	$+\cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) - \sin\phi_s \sin$	$n(\Delta mt]$ ,	(10)
$+ \cos(\delta_{\parallel} - \delta_{s}) \cos(\Delta m t)], \qquad (11)$ $\Im(A_{s}^{*}(t)A_{\perp}(t)) =  A_{s}  A_{\perp} e^{-\Gamma_{s}t} \sin(\delta_{\perp} - \delta_{s}) \cosh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\phi_{s} \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ - \sin\phi_{s} \sin(\Delta m t)], \qquad (12)$ $\Re(A_{s}^{*}(t)A_{0}(t)) =  A_{s}  A_{0} e^{-\Gamma_{s}t}  - \sin(\delta_{0} - \delta_{s}) \sin\phi_{s} \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ - \sin(\delta_{0} - \delta_{s}) \cos\phi_{s} \sin(\Delta m t) + \cos(\delta_{0} - \delta_{s}) \cos(\Delta m t)]. \qquad (13)$		$\Re(A^*_s(t)A_{\parallel}(t))$	-	$ A_s  A$	$ e^{-\Gamma_{a}t}  - \sin(\delta_{\parallel} - \delta_{\parallel}) $	$\delta_s \sin \phi_s \sinh \left(\frac{\Delta \Gamma}{2} t\right) - \sin(\delta_{\parallel})$	$-\delta_s \cos \phi_s \sin(\Delta m t)$	
$\begin{aligned} &\Im(A_s^*(t)A_{\perp}(t)) =  A_s  A_{\perp} e^{-\Gamma_s t} \sin(\delta_{\perp} - \delta_s) \cosh\left(\frac{\Delta\Gamma}{2}t\right) + \cos\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &- \sin\phi_s \sin(\Delta m t) , \end{aligned} (12) \\ &\Re(A_s^*(t)A_0(t)) =  A_s  A_0 e^{-\Gamma_s t}  - \sin(\delta_0 - \delta_s) \sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ &- \sin(\delta_0 - \delta_s) \cos\phi_s \sin(\Delta m t) + \cos(\delta_0 - \delta_s) \cos(\Delta m t) . \end{aligned}$				+ cos(	$\delta_{\parallel} - \delta_s \cos(\Delta m t)$	1		(11)
$= -\sin \phi_s \sin(\Delta m t)], \qquad (12)$ $\Re[A_s^*(t)A_0(t)) =  A_s  A_0 e^{-\Gamma \star t}[-\sin(\delta_0 - \delta_s)\sin \phi_s \sinh\left(\frac{\Delta \Gamma}{2}t\right) \\ -\sin(\delta_0 - \delta_s)\cos \phi_s \sin(\Delta m t) + \cos(\delta_0 - \delta_s)\cos(\Delta m t)]. \qquad (13)$		$\Im(A^*_s(t)A_{\perp}(t))$	-	$ A_s  A$	$_{\perp} e^{-\Gamma_{a}t}\sin(\delta_{\perp}-\delta) $	$\delta_s \left( \cosh \left( \frac{\Delta \Gamma}{2} t \right) + \cos \phi_s \sinh \left( \frac{\Delta \Gamma}{2} t \right) \right)$	$\frac{\Delta \Gamma}{2}$ I)	
$\Re[A_s^*(t)A_0(t)) -  A_s  A_0 e^{-\Gamma \star t}[-\sin(\delta_0 - \delta_s)\sin\phi_s \sinh\left(\frac{\Delta\Gamma}{2}t\right) \\ -\sin(\delta_0 - \delta_s)\cos\phi_s \sin(\Delta m t) + \cos(\delta_0 - \delta_s)\cos(\Delta m t)].$ (13)				— sin ¢	$sin(\Delta mt)$ ,			(12)
$-\sin(\delta_0 - \delta_s)\cos\phi_s\sin(\Delta mt) + \cos(\delta_0 - \delta_s)\cos(\Delta mt)]. \qquad (13)$		$\Re(A^*_{s}(t)A_0(t))$	-	$ A_{\theta}  A$	$_0 e^{-\Gamma st} -\sin(\delta_0-$	$\delta_s \sin \phi_s \sinh \left(\frac{\Delta \Gamma}{2}t\right)$		
			_	— sin(à	$\delta_0 - \delta_s \cos \phi_s \sin(2$	$\Delta mt$ ) + cos( $\delta_0 - \delta_s$ ) cos( $\Delta mt$ )].		(13)

where we have chosen a phase convention such that  $\delta_0 = 0$ . The decay time dependent decay rates for an initial  $\overline{B}_{a}^{0}$  decaying to  $J/\psi\phi$  can be obtained from those above by inserting a factor -1 in front of the terms involving mixing  $(sin(\Delta m_s t) and cos(\Delta m_s t))$ .

#### accounts for ~4% "non-resonant" KK in 12 MeV mass window around phi

![](_page_57_Figure_7.jpeg)

note: S-wave contribution identified by angular distribution, not by KK mass

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add sity

![](_page_58_Picture_0.jpeg)

![](_page_58_Figure_1.jpeg)

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![](_page_58_Picture_4.jpeg)

![](_page_59_Picture_0.jpeg)

#### Flavour tagging

- To measure  $\phi_s$  we need to know the  $B_s^0$  flavour at the production vertex
- ► B<sup>0</sup><sub>s</sub> flavour is determined by **tagging** algorithms LHCb-CONF-2011-003:
  - Opposite Side (**OS**): Decay products of the other b-meson
  - Same Side (SS): particles produced in fragmentation alongside signal B

![](_page_59_Figure_6.jpeg)

- ► Results shown here use OS tagging only. This is optimised and calibrated using the control channel B<sup>+</sup> → J/ $\psi$ K<sup>+</sup>  $\epsilon_{eff}$ (J/ $\psi\phi$ ) =  $\epsilon$ (1 2 $\omega$ )<sup>2</sup> = 2.08 ± 0.41%
- Future analyses will also use the SS tagger.

![](_page_59_Picture_11.jpeg)

![](_page_60_Picture_0.jpeg)

Half of the bandwidth (~1 kHz) given to the muon lines  $p_T$  cuts on muon lines kept very low  $\rightarrow$  trigger efficiency very high Trigger rather stable during the whole period (despite L increased by ~10<sup>5</sup>)

![](_page_60_Figure_3.jpeg)

![](_page_61_Picture_0.jpeg)

- Events are classified in 2D plane: invariant mass, GL
- Evaluate the compatibility of measurement with
  - B only hypothesis [CL<sub>B</sub>]
     → quote observation
  - S+B hypothesis
     [CL<sub>s</sub>=CL<sub>S+B</sub>/CL<sub>B</sub>]
     →quote exclusion limit

![](_page_61_Figure_6.jpeg)

- Calculate **expected limit** using toy MC techniques
  - Shows reach of the measurement, independent of stat. fluctuations
  - Errors of normalization factors and PDF parameters are included as nuisance parameters in limit calculation
- Use pattern of events to calculate **observed limit**

![](_page_61_Picture_13.jpeg)

![](_page_62_Picture_0.jpeg)

- LHCb: maximize B acceptance @ LHC
  - $\rightarrow$  forward spectrometer, 1.9< $\eta$ <4.9
    - B hadrons produced at low angle
    - B pairs are produced in same forward or backward cone → single arm ok

![](_page_62_Figure_6.jpeg)

![](_page_62_Picture_7.jpeg)

![](_page_63_Picture_0.jpeg)

(CDF: |n|<1 ;

D0: |n|<2; CMS/ATLAS:|n|<2.4

## LHCb acceptance

- LHCb: maximize B acceptance @ LHC •  $\rightarrow$  forward spectrometer, 1.9< $\eta$ <4.9
  - B hadrons produced at low angle
  - B pairs are produced in same forward or backward cone  $\rightarrow$  single arm ok

Rough estimate for B acceptance: compare  $B^{\pm} \rightarrow J/\psi K^{\pm}$  yield with CDF / D0

**LHCb**  $(0.037 \text{fb}^{-1})$ Nsignal-12,366±403<sup>stat+syst</sup> CDF<sub>(CMU-CM(U+X))</sub> 19,762±203stat+syst (3.7fb<sup>-1</sup>) Nsignal D0<sub>(Runlla+b)</sub>  $(6.1 \text{ fb}^{-1})$ 

46,803±1099stat+syst Nsignal

![](_page_63_Figure_8.jpeg)

 $m_{J/\psi K^{+}}$  [GeV]

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![](_page_64_Picture_0.jpeg)

## LHCb acceptance

- LHCb: maximize B acceptance @ LHC → forward spectrometer, 1.9<η<4.9</li>
  - B hadrons produced at low angle
  - B pairs are produced in same forward or backward cone → single arm ok

Rough estimate for B acceptance: compare  $B^{\pm} \rightarrow J/\psi K^{\pm}$  yield with CDF / D0

- LHCb N<sup>signal</sup>: 12,366±403<sup>stat+syst</sup> (0.037fb<sup>-1</sup>)
- CMS (from 5.8pb-1)
   N<sup>signal</sup>: 5,818
- ATLAS (from 3.4pb-1)
   N<sup>signal</sup>: 3,080

![](_page_64_Figure_9.jpeg)

scaled

scaled

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![](_page_65_Picture_0.jpeg)

### Likelihood scan in K\*mm

Κ\*μμ

![](_page_65_Figure_3.jpeg)

![](_page_65_Figure_4.jpeg)

 $A_{FB}$ 

(e)  $14.18 < q^2 < 16 \,\mathrm{GeV}^2$ 

(f)  $16 < q^2 < 19 \,\text{GeV}^2$ 

LHCb-CONF-2011-038

Figure 6: Profile-likelihood contour (profiling the background parameters and the signal fraction) showing the difference in log-likelihood between the global minimum and the likelihood at each value of  $A_{FB}$  and  $F_L$  for the seven  $q^2$  bins used in the analysis. Points outside the physical region are not included resulting in the triangular boundary visible in the figures. 11

 $\mathbf{A}_{\mathsf{FB}}$ 

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#### **Johannes Albrecht**

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